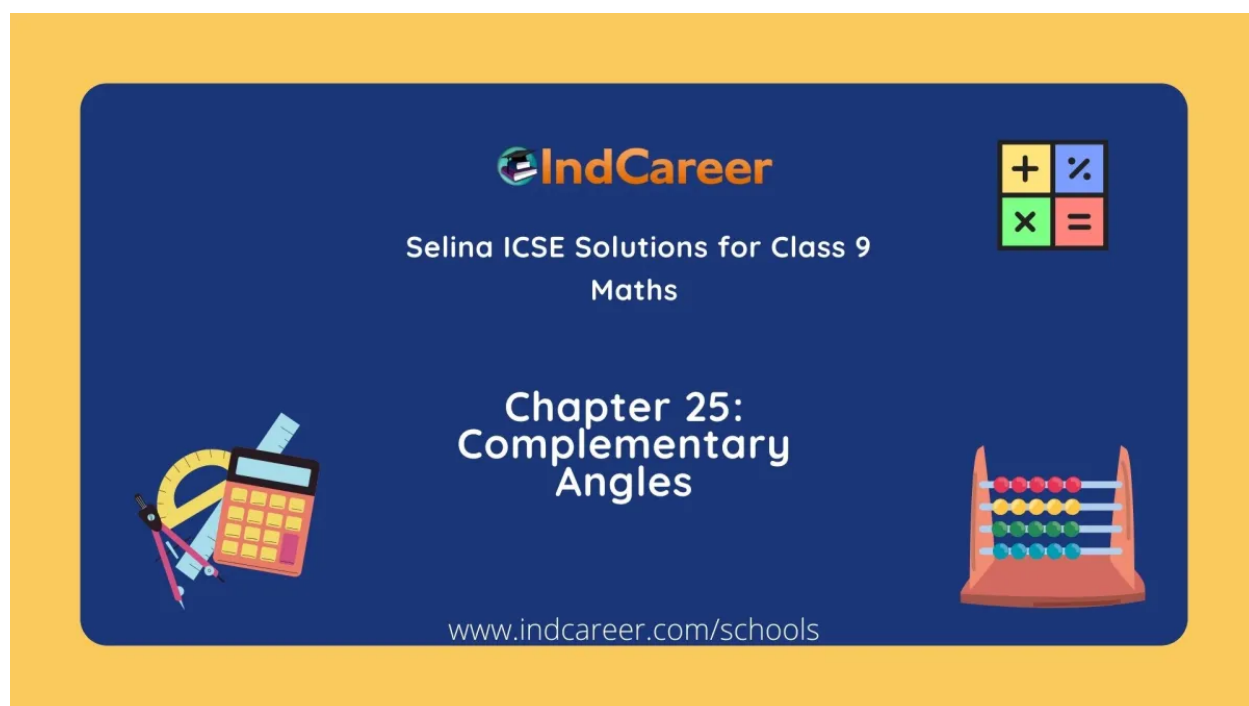


# Selina Class 9 ICSE Solutions Mathematics :

## Chapter 25- Complementary Angles



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# Selina Class 9 ICSE Solutions Mathematics :

## Chapter 25- Complementary Angles

Class 9: Maths Chapter 25 solutions. Complete Class 9 Maths Chapter 25 Notes.

### Selina Class 9 ICSE Solutions Mathematics : Chapter 25- Complementary Angles

Selina 9th Maths Chapter 25, Class 9 Maths Chapter 25 solutions

#### Exercise 25(A)

Solution 1(i):

$$\frac{\cos 22^\circ}{\sin 68^\circ} = \frac{\cos(90^\circ - 68^\circ)}{\sin 68^\circ} = \frac{\sin 68^\circ}{\sin 68^\circ} = 1$$

Solution 1(ii):

$$\frac{\tan 47^\circ}{\cot 43^\circ} = \frac{\tan(90^\circ - 43^\circ)}{\cot 43^\circ} = \frac{\cot 43^\circ}{\cot 43^\circ} = 1$$

Solution 1(iii):

$$\frac{\sec 75^\circ}{\operatorname{cosec} 15^\circ} = \frac{\sec(90^\circ - 15^\circ)}{\operatorname{cosec} 15^\circ} = \frac{\operatorname{cosec} 15^\circ}{\operatorname{cosec} 15^\circ} = 1$$

Solution 1(iv):

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$$\begin{aligned}& \frac{\cos 55^\circ}{\sin 35^\circ} + \frac{\cot 35^\circ}{\tan 55^\circ} \\&= \frac{\cos(90^\circ - 35^\circ)}{\sin 35^\circ} + \frac{\cot(90^\circ - 55^\circ)}{\tan 55^\circ} \\&= \frac{\sin 35^\circ}{\sin 35^\circ} + \frac{\tan 55^\circ}{\tan 55^\circ} \\&= 1 + 1 \\&= 2\end{aligned}$$

**Solution 1(v):**

$$\begin{aligned}& \sin^2 40^\circ - \cos^2 50^\circ \\&= \sin^2 (90^\circ - 50^\circ) - \cos^2 50^\circ \\&= \cos^2 50^\circ - \cos^2 50^\circ \\&= 0\end{aligned}$$

**Solution 1(vi):**

$$\begin{aligned}& \sec^2 18^\circ - \operatorname{cosec}^2 72^\circ \\&= [\sec(90^\circ - 72^\circ)]^2 - \operatorname{cosec}^2 72^\circ \\&= \operatorname{cosec}^2 72^\circ - \operatorname{cosec}^2 72^\circ \\&= 0\end{aligned}$$

**Solution 1(vii):**

$$\begin{aligned}& \sin 15^\circ \cos 15^\circ - \cos 75^\circ \sin 75^\circ \\&= \sin(90^\circ - 75^\circ) \cos 15^\circ - \cos 75^\circ \sin (90^\circ - 15^\circ) \\&= \cos 75^\circ \cos 15^\circ - \cos 75^\circ \cos 15^\circ \\&= 0\end{aligned}$$

**Solution 1(viii):**

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$$\begin{aligned} & \sin 42^\circ \sin 48^\circ - \cos 42^\circ \cos 48^\circ \\ &= \sin(90^\circ - 48^\circ) \sin 48^\circ - \cos(90^\circ - 48^\circ) \cos 48^\circ \\ &= \cos 48^\circ \sin 48^\circ - \sin 48^\circ \cos 48^\circ \\ &= \cos 48^\circ \sin 48^\circ - \cos 48^\circ \sin 48^\circ \\ &= 0 \end{aligned}$$

**Solution 2(i):**

$$\begin{aligned} & \sin(90^\circ - A) \sin A - \cos(90^\circ - A) \cos A \\ &= \cos A \sin A - \sin A \cos A \\ &= 0 \end{aligned}$$

**Solution 2(ii):**

$$\begin{aligned} & \sin^2 35^\circ - \cos^2 55^\circ \\ &= \sin^2 35^\circ - [\cos(90^\circ - 35^\circ)]^2 \\ &= \sin^2 35^\circ - \sin^2 35^\circ \\ &= 0 \end{aligned}$$

**Solution 2(iii):**

$$\begin{aligned} & \frac{\cot 54^\circ}{\tan 36^\circ} + \frac{\tan 20^\circ}{\cot 70^\circ} - 2 \\ &= \frac{\cot(90^\circ - 36^\circ)}{\tan 36^\circ} + \frac{\tan(90^\circ - 70^\circ)}{\cot 70^\circ} - 2 \\ &= \frac{\tan 36^\circ}{\tan 36^\circ} + \frac{\cot 70^\circ}{\cot 70^\circ} - 2 \\ &= 1 + 1 - 2 \\ &= 2 - 2 \\ &= 0 \end{aligned}$$

**Solution 2(iv):**

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$$\begin{aligned}& \frac{2 \tan 53^\circ}{\cot 37^\circ} - \frac{\cot 80^\circ}{\tan 10^\circ} \\&= \frac{2 \tan (90^\circ - 37^\circ)}{\cot 37^\circ} - \frac{\cot (90^\circ - 10^\circ)}{\tan 10^\circ} \\&= \frac{2 \cot 37^\circ}{\cot 37^\circ} - \frac{\tan 10^\circ}{\tan 10^\circ} \\&= 2 - 1 \\&= 1\end{aligned}$$

**Solution 2(v):**

$$\begin{aligned}& \cos^2 25^\circ - \sin^2 65^\circ - \tan^2 45^\circ \\&= [\cos(90^\circ - 65^\circ)]^2 - \sin^2 65^\circ - (\tan 45^\circ)^2 \\&= \sin^2 65^\circ - \sin^2 65^\circ - (1)^2 \\&= 0 - 1 \\&= -1\end{aligned}$$

**Solution 2(vi):**

$$\begin{aligned}& \left( \frac{\sin 77^\circ}{\cos 13^\circ} \right)^2 + \left( \frac{\cos 77^\circ}{\sin 13^\circ} \right)^2 - 2 \cos^2 45^\circ \\&= \left( \frac{\sin (90^\circ - 13^\circ)}{\cos 13^\circ} \right)^2 + \left( \frac{\cos (90^\circ - 13^\circ)}{\sin 13^\circ} \right)^2 - 2 (\cos 45^\circ)^2 \\&= \left( \frac{\cos 13^\circ}{\cos 13^\circ} \right)^2 + \left( \frac{\sin 13^\circ}{\sin 13^\circ} \right)^2 - 2 \left( \frac{1}{\sqrt{2}} \right)^2 \\&= (1)^2 + (1)^2 - 2 \times \frac{1}{2} \\&= 1 + 1 - 1 \\&= 1\end{aligned}$$

**Solution 3(i):**

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L.H.S.

$$= \tan 10^\circ \tan 15^\circ \tan 75^\circ \tan 80^\circ$$

$$= \tan (90^\circ - 80^\circ) \tan (90^\circ - 75^\circ) \tan 75^\circ \tan 80^\circ$$

$$= \cot 80^\circ \cot 75^\circ \tan 75^\circ \tan 80^\circ$$

$$= (\cot 80^\circ \tan 80^\circ)(\cot 75^\circ \tan 75^\circ)$$

$$= (1)(1)$$

$$= 1$$

$$= \text{R.H.S.}$$

**Solution 3(ii):**

L.H.S.

$$= \sin 42^\circ \sec 48^\circ + \cos 42^\circ \operatorname{cosec} 48^\circ$$

$$= \sin(90^\circ - 48^\circ) \times \frac{1}{\cos 48^\circ} + \cos(90^\circ - 48^\circ) \times \frac{1}{\sin 48^\circ}$$

$$= \cos 48^\circ \times \frac{1}{\cos 48^\circ} + \sin 48^\circ \times \frac{1}{\sin 48^\circ}$$

$$= 1 + 1$$

$$= 2$$

$$= \text{R.H.S.}$$

**Solution 4:**

$$(i) \sin 59^\circ + \tan 63^\circ$$

$$= \sin(90^\circ - 31^\circ) + \tan(90^\circ - 27^\circ)$$

$$= \cos 31^\circ + \cot 27^\circ$$

$$(ii) \operatorname{cosec} 68^\circ + \cot 72^\circ$$

$$= \operatorname{cosec} (90^\circ - 22^\circ) + \cot(90^\circ - 18^\circ)$$

$$= \sec 22^\circ + \tan 18^\circ$$

$$(iii) \cos 74^\circ + \sec 67^\circ$$

$$= \cos(90^\circ - 16^\circ) + \sec(90^\circ - 23^\circ)$$

$$= \sin 16^\circ + \operatorname{cosec} 23^\circ$$

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**Solution 5:**

(i) We know that for a triangle  $\Delta ABC$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\frac{\angle B + \angle A}{2} = 90^\circ - \frac{\angle C}{2}$$

$$\begin{aligned}\sin\left(\frac{A+B}{2}\right) &= \sin\left(90^\circ - \frac{C}{2}\right) \\ &= \cos\left(\frac{C}{2}\right)\end{aligned}$$

(ii) We know that for a triangle  $\Delta ABC$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle B + \angle C = 180^\circ - \angle A$$

$$\frac{\angle B + \angle C}{2} = 90^\circ - \frac{\angle A}{2}$$

$$\begin{aligned}\tan\left(\frac{B+C}{2}\right) &= \tan\left(90^\circ - \frac{A}{2}\right) \\ &= \cot\left(\frac{A}{2}\right)\end{aligned}$$

**Solution 6:**

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(i)

$$\begin{aligned} & 3 \frac{\sin 72^\circ}{\cos 18^\circ} - \frac{\sec 32^\circ}{\cos \sec 58^\circ} \\ &= 3 \frac{\sin(90^\circ - 18^\circ)}{\cos 18^\circ} - \frac{\sec(90^\circ - 58^\circ)}{\cos \sec 58^\circ} \\ &= 3 \frac{\cos 18^\circ}{\cos 18^\circ} - \frac{\cos \sec 58^\circ}{\cos \sec 58^\circ} = 3 - 1 = 2 \end{aligned}$$

(ii)  $3 \cos 80^\circ \operatorname{cosec} 10^\circ + 2 \cos 59^\circ \operatorname{cosec} 31^\circ$

$$\begin{aligned} &= 3 \cos(90^\circ - 10^\circ) \operatorname{cosec} 10^\circ + 2 \cos(90^\circ - 31^\circ) \operatorname{cosec} 31^\circ \\ &= 3 \sin 10^\circ \operatorname{cosec} 10^\circ + 2 \sin 31^\circ \operatorname{cosec} 31^\circ \\ &= 3 + 2 = 5 \end{aligned}$$

(iii)  $\frac{\sin 80^\circ}{\cos 10^\circ} + \sin 59^\circ \sec 31^\circ$

$$\begin{aligned} &= \frac{\sin(90^\circ - 10^\circ)}{\cos 10^\circ} + \sin(90^\circ - 31^\circ) \sec 31^\circ \\ &= \frac{\cos 10^\circ}{\cos 10^\circ} + \frac{\cos 31^\circ}{\cos 31^\circ} \\ &= 1 + 1 = 2 \end{aligned}$$

(iv)  $\tan(55^\circ - A) - \cot(35^\circ + A)$

$$\begin{aligned} &= \tan[90^\circ - (35^\circ + A)] - \cot(35^\circ + A) \\ &= \cot(35^\circ + A) - \cot(35^\circ + A) \\ &= 0 \end{aligned}$$

(v)  $\operatorname{cosec}(65^\circ + A) - \sec(25^\circ - A)$

$$\begin{aligned} &= \operatorname{cosec}[90^\circ - (25^\circ - A)] - \sec(25^\circ - A) \\ &= \sec(25^\circ - A) - \sec(25^\circ - A) \\ &= 0 \end{aligned}$$

(vi)  $2 \frac{\tan 57^\circ}{\cot 33^\circ} - \frac{\cot 70^\circ}{\tan 20^\circ} - \sqrt{2} \cos 45^\circ$

$$\begin{aligned} &= 2 \frac{\tan(90^\circ - 33^\circ)}{\cot 33^\circ} - \frac{\cot(90^\circ - 20^\circ)}{\tan 20^\circ} - \sqrt{2} \left( \frac{1}{\sqrt{2}} \right) \\ &= 2 \frac{\cot 33^\circ}{\cot 33^\circ} - \frac{\tan 20^\circ}{\tan 20^\circ} - 1 \\ &= 2 - 1 - 1 \\ &= 0 \end{aligned}$$

$$\begin{aligned}
 \text{(vii)} \quad & \frac{\cot^2 41^\circ}{\tan^2 49^\circ} - 2 \frac{\sin^2 75^\circ}{\cos^2 15^\circ} \\
 &= \frac{[\cot(90^\circ - 49^\circ)]^2}{\tan^2 49^\circ} - 2 \frac{[\sin(90^\circ - 15^\circ)]^2}{\cos^2 15^\circ} \\
 &= \frac{\tan^2 49^\circ}{\tan^2 49^\circ} - 2 \frac{\cos^2 15^\circ}{\cos^2 15^\circ} \\
 &= 1 - 2 = -1 \\
 \text{(viii)} \quad & \frac{\cos 70^\circ}{\sin 20^\circ} + \frac{\cos 59^\circ}{\sin 31^\circ} - 8 \sin^2 30^\circ \\
 &= \frac{\cos(90^\circ - 20^\circ)}{\sin 20^\circ} + \frac{\cos(90^\circ - 31^\circ)}{\sin 31^\circ} - 8 \left(\frac{1}{2}\right)^2 \\
 &= \frac{\sin 20^\circ}{\sin 20^\circ} + \frac{\sin 31^\circ}{\sin 31^\circ} - 2 \\
 &= 1 + 1 - 2 = 0 \\
 \text{(ix)} \quad & 14 \sin 30^\circ + 6 \cos 60^\circ - 5 \tan 45^\circ \\
 &= 14 \left(\frac{1}{2}\right) + 6 \left(\frac{1}{2}\right) - 5(1) \\
 &= 7 + 3 - 5 = 5
 \end{aligned}$$

#### Solution 7:

Since  $\triangle ABC$  is a right-angled triangle, right-angled at B,

$$A + C = 90^\circ$$

$$\begin{aligned}
 \therefore & \frac{\sec A \cdot \sin C - \tan A \cdot \tan C}{\sin B} \\
 &= \frac{\sec A(90^\circ - C) \sin C - \tan(90^\circ - C) \tan C}{\sin 90^\circ} \\
 &= \frac{\operatorname{cosec} C \sin C - \cot C \tan C}{1} \\
 &= \frac{1}{\sin C} \times \sin C - \frac{1}{\tan C} \times \tan C \\
 &= 1 - 1 \\
 &= 0
 \end{aligned}$$

#### Solution 8(i):

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$$\sin (90^{\circ} - 3A) \cdot \operatorname{cosec} 42^{\circ} = 1$$

$$\Rightarrow \sin (90^{\circ} - 3A) = \frac{1}{\operatorname{cosec} 42^{\circ}}$$

$$\Rightarrow \cos 3A = \frac{1}{\operatorname{cosec} (90^{\circ} - 48^{\circ})}$$

$$\Rightarrow \cos 3A = \frac{1}{\sec 48^{\circ}}$$

$$\Rightarrow \cos 3A = \cos 48^{\circ}$$

$$\Rightarrow 3A = 48^{\circ}$$

$$\Rightarrow A = 16^{\circ}$$

**Solution 8(ii):**

$$\cos (90^{\circ} - 3A) \cdot \sec 77^{\circ} = 1$$

$$\Rightarrow \cos (90^{\circ} - 3A) = \frac{1}{\sec 77^{\circ}}$$

$$\Rightarrow \sin 3A = \frac{1}{\sec (90^{\circ} - 12^{\circ})}$$

$$\Rightarrow \sin 3A = \frac{1}{\operatorname{cosec} 12^{\circ}}$$

$$\Rightarrow \sin 3A = \sin 12^{\circ}$$

$$\Rightarrow 3A = 12^{\circ}$$

$$\Rightarrow A = 3^{\circ}$$



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- Chapter 3 - Compound Interest (Using Formula)
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- Chapter 5- Factorisation
- Chapter 6 - Simultaneous (Linear) Equations (Including Problems)
- Chapter 7- Indices (Exponents)
- Chapter 8- Logarithms
- Chapter 9- Triangles [Congruency in Triangles]
- Chapter 10- Isosceles Triangles
- Chapter 11- Inequalities
- Chapter 12- Mid-point and Its Converse [ Including Intercept Theorem]
- Chapter 13- Pythagoras Theorem [Proof and Simple Applications with Converse]
- Chapter 14- Rectilinear Figures [Quadrilaterals: Parallelogram, Rectangle, Rhombus, Square and Trapezium]
- Chapter 15- Construction of Polygons
- Chapter 16- Area Theorems [Proof and Use]

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- Chapter 17- Circle
- Chapter 18- Statistics
- Chapter 19- Mean and Median
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- Chapter 26- Co-ordinate Geometry
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