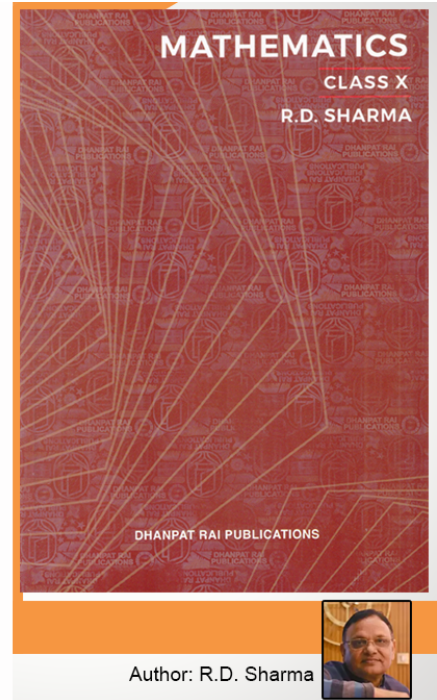


Class 10 - Chapter 5 Trigonometric Ratios



RD Sharma Solutions for Class 10 Maths Chapter 5–Trigonometric Ratios

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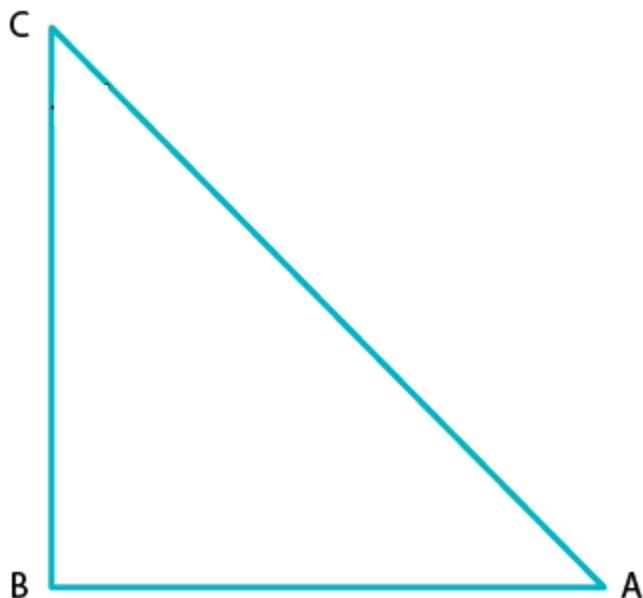
RD Sharma 10th Maths Chapter 5, Class 10 Maths Chapter 5 solutions

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Exercise 5.1 Page No: 5.23

1. In each of the following, one of the six trigonometric ratios is given. Find the values of the other trigonometric ratios.



(i) $\sin A = 2/3$

Solution:

We have,

$$\sin A = 2/3 \dots\dots\dots (1)$$

As we know, by sin definition;

$$\sin A = \text{Perpendicular} / \text{Hypotenuse} = 2/3 \dots\dots(2)$$

By comparing eq. (1) and (2), we have

Opposite side = 2 and Hypotenuse = 3

Now, on using Pythagoras theorem in ΔABC

$$AC^2 = AB^2 + BC^2$$

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Putting the values of perpendicular side (BC) and hypotenuse (AC) and for the base side as (AB), we get

$$\Rightarrow 3^2 = AB^2 + 2^2$$

$$AB^2 = 3^2 - 2^2$$

$$AB^2 = 9 - 4$$

$$AB^2 = 5$$

$$AB = \sqrt{5}$$

Hence, Base = $\sqrt{5}$

By definition,

$$\cos A = \text{Base/Hypotenuse}$$

$$\Rightarrow \cos A = \sqrt{5}/3$$

Since, cosec A = $1/\sin A = \text{Hypotenuse/Perpendicular}$

$$\Rightarrow \text{cosec A} = 3/2$$

And, sec A = Hypotenuse/Base

$$\Rightarrow \sec A = 3/\sqrt{5}$$

And, tan A = Perpendicular/Base

$$\Rightarrow \tan A = 2/\sqrt{5}$$

And, cot A = $1/\tan A = \text{Base/Perpendicular}$

$$\Rightarrow \cot A = \sqrt{5}/2$$

(ii) $\cos A = 4/5$

Solution:

We have,

$$\cos A = 4/5 \dots\dots\dots (1)$$

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As we know, by cos definition

$$\cos A = \text{Base}/\text{Hypotenuse} \dots (2)$$

By comparing eq. (1) and (2), we get

$$\text{Base} = 4 \text{ and Hypotenuse} = 5$$

Now, using Pythagoras theorem in ΔABC

$$AC^2 = AB^2 + BC^2$$

Putting the value of base (AB) and hypotenuse (AC) and for the perpendicular (BC), we get

$$5^2 = 4^2 + BC^2$$

$$BC^2 = 5^2 - 4^2$$

$$BC^2 = 25 - 16$$

$$BC^2 = 9$$

$$BC = 3$$

Hence, Perpendicular = 3

By definition,

$$\sin A = \text{Perpendicular}/\text{Hypotenuse}$$

$$\Rightarrow \sin A = 3/5$$

$$\text{Then, cosec } A = 1/\sin A$$

$$\Rightarrow \text{cosec } A = 1/(3/5) = 5/3 = \text{Hypotenuse}/\text{Perpendicular}$$

$$\text{And, sec } A = 1/\cos A$$

$$\Rightarrow \text{sec } A = \text{Hypotenuse}/\text{Base}$$

$$\text{sec } A = 5/4$$

$$\text{And, tan } A = \text{Perpendicular}/\text{Base}$$

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$$\Rightarrow \tan A = 3/4$$

Next, $\cot A = 1/\tan A = \text{Base/Perpendicular}$

$$\therefore \cot A = 4/3$$

$$\text{(iii) } \tan \theta = 11/1$$

Solution:

We have, $\tan \theta = 11 \dots \dots \dots (1)$

By definition,

$$\tan \theta = \text{Perpendicular/ Base} \dots (2)$$

On Comparing eq. (1) and (2), we get;

$$\text{Base} = 1 \text{ and Perpendicular} = 11$$

Now, using Pythagoras theorem in ΔABC .

$$AC^2 = AB^2 + BC^2$$

Putting the value of base (AB) and perpendicular (BC) to get hypotenuse(AC), we get;

$$AC^2 = 1^2 + 11^2$$

$$AC^2 = 1 + 121$$

$$AC^2 = 122$$

$$AC = \sqrt{122}$$

Hence, hypotenuse = $\sqrt{122}$

By definition,

$$\sin \theta = \text{Perpendicular/Hypotenuse}$$

$$\Rightarrow \sin \theta = 11/\sqrt{122}$$

$$\text{And, } \operatorname{cosec} \theta = 1/\sin \theta$$

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$$\Rightarrow \operatorname{cosec} \theta = \sqrt{122/11}$$

Next, $\cos \theta = \text{Base} / \text{Hypotenuse}$

$$\Rightarrow \cos \theta = 1/\sqrt{122}$$

And, $\sec \theta = 1/\cos \theta$

$$\Rightarrow \sec \theta = \sqrt{122/1} = \sqrt{122}$$

And, $\cot \theta = 1/\tan \theta$

$$\therefore \cot \theta = 1/11$$

(iv) $\sin \theta = 11/15$

Solution:

We have, $\sin \theta = 11/15$ (1)

By definition,

$\sin \theta = \text{Perpendicular} / \text{Hypotenuse}$ (2)

On Comparing eq. (1) and (2), we get;

Perpendicular = 11 and Hypotenuse = 15

Now, using Pythagoras theorem in ΔABC

$$AC^2 = AB^2 + BC^2$$

Putting the value of perpendicular (BC) and hypotenuse (AC) to get the base (AB), we have

$$15^2 = AB^2 + 11^2$$

$$AB^2 = 15^2 - 11^2$$

$$AB^2 = 225 - 121$$

$$AB^2 = 104$$

$$AB = \sqrt{104}$$

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$$AB = \sqrt{(2 \times 2 \times 2 \times 13)}$$

$$AB = 2\sqrt{(2 \times 13)}$$

$$AB = 2\sqrt{26}$$

$$\text{Hence, Base} = 2\sqrt{26}$$

By definition,

$$\cos \theta = \text{Base/Hypotenuse}$$

$$\therefore \cos \theta = 2\sqrt{26}/15$$

$$\text{And, cosec } \theta = 1/\sin \theta$$

$$\therefore \text{cosec } \theta = 15/11$$

$$\text{And, sec } \theta = \text{Hypotenuse/Base}$$

$$\therefore \text{sec } \theta = 15/2\sqrt{26}$$

$$\text{And, tan } \theta = \text{Perpendicular/Base}$$

$$\therefore \text{tan } \theta = 11/2\sqrt{26}$$

$$\text{And, cot } \theta = \text{Base/Perpendicular}$$

$$\therefore \text{cot } \theta = 2\sqrt{26}/11$$

$$\text{(v) tan } \alpha = 5/12$$

Solution:

$$\text{We have, tan } \alpha = 5/12 \dots (1)$$

By definition,

$$\text{tan } \alpha = \text{Perpendicular/Base} \dots (2)$$

On Comparing eq. (1) and (2), we get

$$\text{Base} = 12 \text{ and Perpendicular side} = 5$$

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Now, using Pythagoras theorem in ΔABC

$$AC^2 = AB^2 + BC^2$$

Putting the value of base (AB) and the perpendicular (BC) to get hypotenuse (AC), we have

$$AC^2 = 12^2 + 5^2$$

$$AC^2 = 144 + 25$$

$$AC^2 = 169$$

$$AC = 13 \text{ [After taking sq root on both sides]}$$

Hence, Hypotenuse = 13

By definition,

$\sin \alpha = \text{Perpendicular/Hypotenuse}$

$$\therefore \sin \alpha = 5/13$$

And, $\operatorname{cosec} \alpha = \text{Hypotenuse/Perpendicular}$

$$\therefore \operatorname{cosec} \alpha = 13/5$$

And, $\cos \alpha = \text{Base/Hypotenuse}$

$$\therefore \cos \alpha = 12/13$$

And, $\sec \alpha = 1/\cos \alpha$

$$\therefore \sec \alpha = 13/12$$

And, $\tan \alpha = \sin \alpha/\cos \alpha$

$$\therefore \tan \alpha = 5/12$$

Since, $\cot \alpha = 1/\tan \alpha$

$$\therefore \cot \alpha = 12/5$$

$$\text{(vi) } \sin \theta = \sqrt{3}/2$$

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Solution:

We have, $\sin \theta = \sqrt{3}/2$ (1)

By definition,

$\sin \theta = \text{Perpendicular} / \text{Hypotenuse}$(2)

On Comparing eq. (1) and (2), we get;

Perpendicular = $\sqrt{3}$ and Hypotenuse = 2

Now, using Pythagoras theorem in ΔABC

$$AC^2 = AB^2 + BC^2$$

Putting the value of perpendicular (BC) and hypotenuse (AC) and get the base (AB), we get;

$$2^2 = AB^2 + (\sqrt{3})^2$$

$$AB^2 = 2^2 - (\sqrt{3})^2$$

$$AB^2 = 4 - 3$$

$$AB^2 = 1$$

$$AB = 1$$

Thus, Base = 1

By definition,

$\cos \theta = \text{Base} / \text{Hypotenuse}$

$$\therefore \cos \theta = 1/2$$

And, $\text{cosec } \theta = 1/\sin \theta$

Or $\text{cosec } \theta = \text{Hypotenuse} / \text{Perpendicular}$

$$\therefore \text{cosec } \theta = 2/\sqrt{3}$$

And, $\sec \theta = \text{Hypotenuse} / \text{Base}$

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$$\therefore \sec \theta = 2/1$$

And, $\tan \theta = \text{Perpendicular}/\text{Base}$

$$\therefore \tan \theta = \sqrt{3}/1$$

And, $\cot \theta = \text{Base}/\text{Perpendicular}$

$$\therefore \cot \theta = 1/\sqrt{3}$$

(vii) $\cos \theta = 7/25$

Solution:

We have, $\cos \theta = 7/25$ (1)

By definition,

$$\cos \theta = \text{Base}/\text{Hypotenuse}$$

On Comparing eq. (1) and (2), we get;

$$\text{Base} = 7 \text{ and Hypotenuse} = 25$$

Now, using Pythagoras theorem in ΔABC

$$AC^2 = AB^2 + BC^2$$

Putting the value of base (AB) and hypotenuse (AC) to get the perpendicular (BC)

$$25^2 = 7^2 + BC^2$$

$$BC^2 = 25^2 - 7^2$$

$$BC^2 = 625 - 49$$

$$BC^2 = 576$$

$$BC = \sqrt{576}$$

$$BC = 24$$

Hence, Perpendicular side = 24

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By definition,

$\sin \theta = \text{perpendicular/Hypotenuse}$

$$\therefore \sin \theta = 24/25$$

Since, $\operatorname{cosec} \theta = 1/\sin \theta$

Also, $\operatorname{cosec} \theta = \text{Hypotenuse/Perpendicular}$

$$\therefore \operatorname{cosec} \theta = 25/24$$

Since, $\sec \theta = 1/\operatorname{cosec} \theta$

Also, $\sec \theta = \text{Hypotenuse/Base}$

$$\therefore \sec \theta = 25/7$$

Since, $\tan \theta = \text{Perpendicular/Base}$

$$\therefore \tan \theta = 24/7$$

Now, $\cot \theta = 1/\tan \theta$

So, $\cot \theta = \text{Base/Perpendicular}$

$$\therefore \cot \theta = 7/24$$

(viii) $\tan \theta = 8/15$

Solution:

We have, $\tan \theta = 8/15$ (1)

By definition,

$\tan \theta = \text{Perpendicular/Base}$ (2)

On Comparing eq. (1) and (2), we get;

Base = 15 and Perpendicular = 8

Now, using Pythagoras theorem in ΔABC

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$$AC^2 = 15^2 + 8^2$$

$$AC^2 = 225 + 64$$

$$AC^2 = 289$$

$$AC = \sqrt{289}$$

$$AC = 17$$

Hence, Hypotenuse = 17

By definition,

Since, $\sin \theta = \text{perpendicular/Hypotenuse}$

$$\therefore \sin \theta = 8/17$$

Since, $\text{cosec } \theta = 1/\sin \theta$

Also, $\text{cosec } \theta = \text{Hypotenuse/Perpendicular}$

$$\therefore \text{cosec } \theta = 17/8$$

Since, $\cos \theta = \text{Base/Hypotenuse}$

$$\therefore \cos \theta = 15/17$$

Since, $\sec \theta = 1/\cos \theta$

Also, $\sec \theta = \text{Hypotenuse/Base}$

$$\therefore \sec \theta = 17/15$$

Since, $\cot \theta = 1/\tan \theta$

Also, $\cot \theta = \text{Base/Perpendicular}$

$$\therefore \cot \theta = 15/8$$

$$\text{(ix) } \cot \theta = 12/5$$

Solution:

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We have, $\cot \theta = 12/5$ (1)

By definition,

$$\cot \theta = 1/\tan \theta$$

$$\cot \theta = \text{Base/Perpendicular} \dots\dots (2)$$

On Comparing eq. (1) and (2), we have

$$\text{Base} = 12 \text{ and Perpendicular side} = 5$$

Now, using Pythagoras theorem in ΔABC

$$AC^2 = AB^2 + BC^2$$

Putting the value of base (AB) and perpendicular (BC) to get the hypotenuse (AC);

$$AC^2 = 12^2 + 5^2$$

$$AC^2 = 144 + 25$$

$$AC^2 = 169$$

$$AC = \sqrt{169}$$

$$AC = 13$$

Hence, Hypotenuse = 13

By definition,

Since, $\sin \theta = \text{perpendicular/Hypotenuse}$

$$\therefore \sin \theta = 5/13$$

Since, $\text{cosec } \theta = 1/\sin \theta$

Also, $\text{cosec } \theta = \text{Hypotenuse/Perpendicular}$

$$\therefore \text{cosec } \theta = 13/5$$

Since, $\cos \theta = \text{Base/Hypotenuse}$

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$$\therefore \cos \theta = 12/13$$

Since, $\sec \theta = 1/\cos \theta$

Also, $\sec \theta = \text{Hypotenuse}/\text{Base}$

$$\therefore \sec \theta = 13/12$$

Since, $\tan \theta = 1/\cot \theta$

Also, $\tan \theta = \text{Perpendicular}/\text{Base}$

$$\therefore \tan \theta = 5/12$$

$$\text{(x) } \sec \theta = 13/5$$

Solution:

We have, $\sec \theta = 13/5$ (1)

By definition,

$$\sec \theta = \text{Hypotenuse}/\text{Base}..... (2)$$

On Comparing eq. (1) and (2), we get

Base = 5 and Hypotenuse = 13

Now, using Pythagoras theorem in ΔABC

$$AC^2 = AB^2 + BC^2$$

And. putting the value of base side (AB) and hypotenuse (AC) to get the perpendicular side (BC)

$$13^2 = 5^2 + BC^2$$

$$BC^2 = 13^2 - 5^2$$

$$BC^2 = 169 - 25$$

$$BC^2 = 144$$

$$BC = \sqrt{144}$$

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$$BC = 12$$

Hence, Perpendicular = 12

By definition,

Since, $\sin \theta = \text{perpendicular/Hypotenuse}$

$$\therefore \sin \theta = 12/13$$

Since, $\text{cosec } \theta = 1/\sin \theta$

Also, $\text{cosec } \theta = \text{Hypotenuse/Perpendicular}$

$$\therefore \text{cosec } \theta = 13/12$$

Since, $\cos \theta = 1/\sec \theta$

Also, $\cos \theta = \text{Base/Hypotenuse}$

$$\therefore \cos \theta = 5/13$$

Since, $\tan \theta = \text{Perpendicular/Base}$

$$\therefore \tan \theta = 12/5$$

Since, $\cot \theta = 1/\tan \theta$

Also, $\cot \theta = \text{Base/Perpendicular}$

$$\therefore \cot \theta = 5/12$$

$$\text{(xi) cosec } \theta = \sqrt{10}$$

Solution:

$$\text{We have, cosec } \theta = \sqrt{10}/1 \dots\dots\dots (1)$$

By definition,

$$\text{cosec } \theta = \text{Hypotenuse/ Perpendicular} \dots\dots\dots(2)$$

$$\text{And, cosec } \theta = 1/\sin \theta$$

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On comparing eq.(1) and(2), we get

Perpendicular side = 1 and Hypotenuse = $\sqrt{10}$

Now, using Pythagoras theorem in ΔABC

$$AC^2 = AB^2 + BC^2$$

Putting the value of perpendicular (BC) and hypotenuse (AC) to get the base side (AB)

$$(\sqrt{10})^2 = AB^2 + 1^2$$

$$AB^2 = (\sqrt{10})^2 - 1^2$$

$$AB^2 = 10 - 1$$

$$AB = \sqrt{9}$$

$$AB = 3$$

So, Base side = 3

By definition,

Since, $\sin \theta = \text{Perpendicular/Hypotenuse}$

$$\therefore \sin \theta = 1/\sqrt{10}$$

Since, $\cos \theta = \text{Base/Hypotenuse}$

$$\therefore \cos \theta = 3/\sqrt{10}$$

Since, $\sec \theta = 1/\cos \theta$

Also, $\sec \theta = \text{Hypotenuse/Base}$

$$\therefore \sec \theta = \sqrt{10}/3$$

Since, $\tan \theta = \text{Perpendicular/Base}$

$$\therefore \tan \theta = 1/3$$

Since, $\cot \theta = 1/\tan \theta$

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$$\therefore \cot \theta = 3/1$$

(xii) $\cos \theta = 12/15$

Solution:

We have; $\cos \theta = 12/15$ (1)

By definition,

$$\cos \theta = \text{Base/Hypotenuse} \dots\dots\dots (2)$$

By comparing eq. (1) and (2), we get;

$$\text{Base} = 12 \text{ and Hypotenuse} = 15$$

Now, using Pythagoras theorem in ΔABC , we get

$$AC^2 = AB^2 + BC^2$$

Putting the value of base (AB) and hypotenuse (AC) to get the perpendicular (BC);

$$15^2 = 12^2 + BC^2$$

$$BC^2 = 15^2 - 12^2$$

$$BC^2 = 225 - 144$$

$$BC^2 = 81$$

$$BC = \sqrt{81}$$

$$BC = 9$$

So, Perpendicular = 9

By definition,

Since, $\sin \theta = \text{perpendicular/Hypotenuse}$

$$\therefore \sin \theta = 9/15 = 3/5$$

Since, $\text{cosec } \theta = 1/\sin \theta$

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Also, $\operatorname{cosec} \theta = \text{Hypotenuse/Perpendicular}$

$$\therefore \operatorname{cosec} \theta = 15/9 = 5/3$$

Since, $\sec \theta = 1/\cos \theta$

Also, $\sec \theta = \text{Hypotenuse/Base}$

$$\therefore \sec \theta = 15/12 = 5/4$$

Since, $\tan \theta = \text{Perpendicular/Base}$

$$\therefore \tan \theta = 9/12 = 3/4$$

Since, $\cot \theta = 1/\tan \theta$

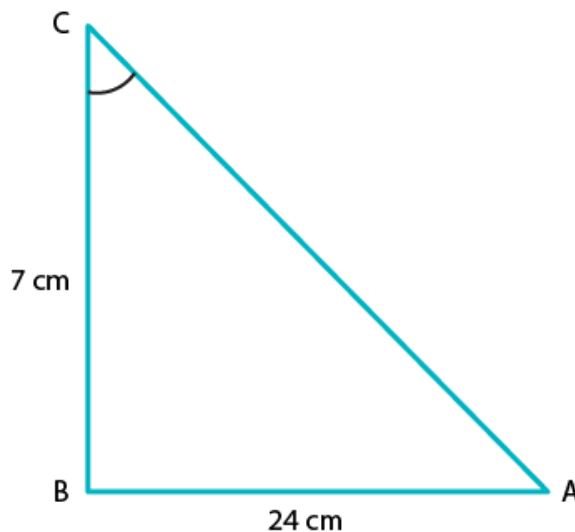
Also, $\cot \theta = \text{Base/Perpendicular}$

$$\therefore \cot \theta = 12/9 = 4/3$$

2. In a $\triangle ABC$, right angled at B, $AB = 24 \text{ cm}$, $BC = 7 \text{ cm}$. Determine

(i) $\sin A$, $\cos A$ (ii) $\sin C$, $\cos C$

Solution:



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(i) Given: In $\triangle ABC$, $AB = 24$ cm, $BC = 7$ cm and $\angle ABC = 90^\circ$

To find: $\sin A$, $\cos A$

By using Pythagoras theorem in $\triangle ABC$ we have

$$AC^2 = AB^2 + BC^2$$

$$AC^2 = 24^2 + 7^2$$

$$AC^2 = 576 + 49$$

$$AC^2 = 625$$

$$AC = \sqrt{625}$$

$$AC = 25$$

Hence, Hypotenuse = 25

By definition,

$\sin A = \frac{\text{Perpendicular side opposite to angle } A}{\text{Hypotenuse}}$

$$\sin A = \frac{BC}{AC}$$

$$\sin A = \frac{7}{25}$$

And,

$\cos A = \frac{\text{Base side adjacent to angle } A}{\text{Hypotenuse}}$

$$\cos A = \frac{AB}{AC}$$

$$\cos A = \frac{24}{25}$$

(ii) Given: In $\triangle ABC$, $AB = 24$ cm and $BC = 7$ cm and $\angle ABC = 90^\circ$

To find: $\sin C$, $\cos C$

By using Pythagoras theorem in $\triangle ABC$ we have

$$AC^2 = AB^2 + BC^2$$

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$$AC^2 = 24^2 + 7^2$$

$$AC^2 = 576 + 49$$

$$AC^2 = 625$$

$$AC = \sqrt{625}$$

$$AC = 25$$

Hence, Hypotenuse = 25

By definition,

$\sin C = \frac{\text{Perpendicular side opposite to angle C}}{\text{Hypotenuse}}$

$$\sin C = \frac{AB}{AC}$$

$$\sin C = \frac{24}{25}$$

And,

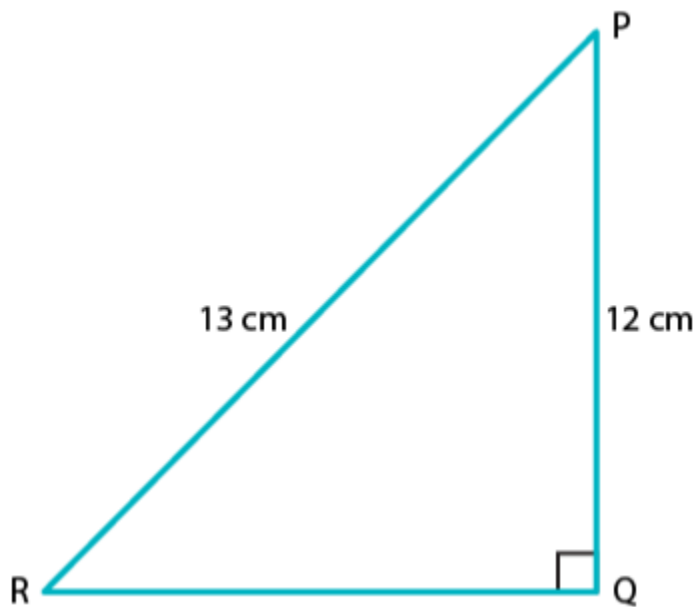
$\cos C = \frac{\text{Base side adjacent to angle C}}{\text{Hypotenuse}}$

$$\cos A = \frac{BC}{AC}$$

$$\cos A = \frac{7}{25}$$

3. In fig. 5.37, find $\tan P$ and $\cot R$. Is $\tan P = \cot R$?

Solution:



By using Pythagoras theorem in $\triangle PQR$, we have

$$PR^2 = PQ^2 + QR^2$$

Putting the length of given side PR and PQ in the above equation

$$13^2 = 12^2 + QR^2$$

$$QR^2 = 13^2 - 12^2$$

$$QR^2 = 169 - 144$$

$$QR^2 = 25$$

$$QR = \sqrt{25} = 5$$

By definition,

$\tan P = \frac{\text{Perpendicular side opposite to } P}{\text{Base side adjacent to angle } P}$

$$\tan P = \frac{QR}{PQ}$$

$$\tan P = \frac{5}{12} \dots\dots\dots (1)$$

And,

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$\cot R = \text{Base/Perpendicular}$

$\cot R = QR/PQ$

$\cot R = 5/12 \dots (2)$

When comparing equation (1) and (2), we can see that R.H.S of both the equation is equal.

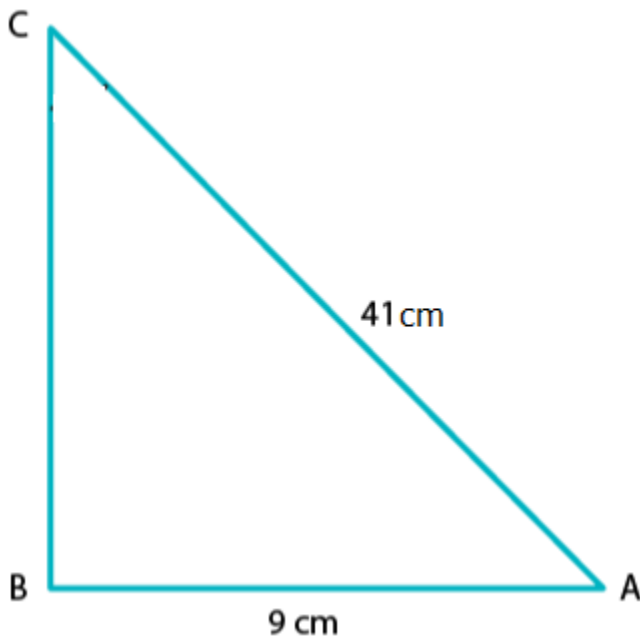
Therefore, L.H.S of both equations should also be equal.

$\therefore \tan P = \cot R$

Yes, $\tan P = \cot R = 5/12$

4. If $\sin A = 9/41$, compute $\cos A$ and $\tan A$.

Solution:



Given that, $\sin A = 9/41 \dots\dots\dots (1)$

Required to find: $\cos A$, $\tan A$

By definition, we know that

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$\sin A = \text{Perpendicular} / \text{Hypotenuse} \dots \dots \dots (2)$

On Comparing eq. (1) and (2), we get;

Perpendicular side = 9 and Hypotenuse = 41

Let's construct $\triangle ABC$ as shown below,

And, here the length of base AB is unknown.

Thus, by using Pythagoras theorem in $\triangle ABC$, we get;

$$AC^2 = AB^2 + BC^2$$

$$41^2 = AB^2 + 9^2$$

$$AB^2 = 41^2 - 9^2$$

$$AB^2 = 168 - 81$$

$$AB = 1600$$

$$AB = \sqrt{1600}$$

$$AB = 40$$

\Rightarrow Base of triangle ABC, AB = 40

We know that,

$$\cos A = \text{Base} / \text{Hypotenuse}$$

$$\cos A = AB / AC$$

$$\cos A = 40 / 41$$

And,

$$\tan A = \text{Perpendicular} / \text{Base}$$

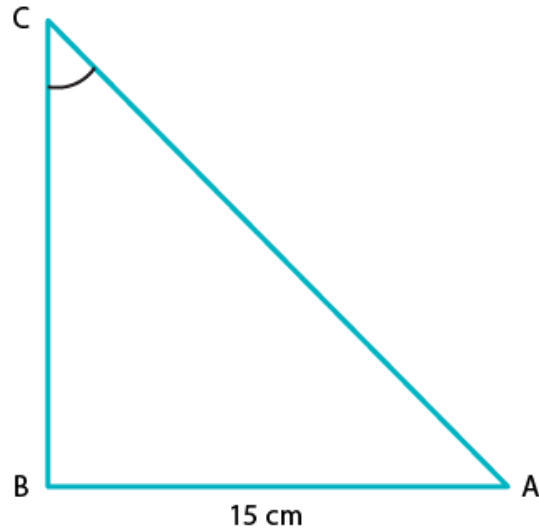
$$\tan A = BC / AB$$

$$\tan A = 9 / 40$$

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5. Given $15\cot A = 8$, find $\sin A$ and $\sec A$.

Solution



We have, $15\cot A = 8$

Required to find: $\sin A$ and $\sec A$

As, $15\cot A = 8$

$$\Rightarrow \cot A = 8/15 \dots\dots(1)$$

And we know,

$$\cot A = 1/\tan A$$

Also by definition,

$$\cot A = \text{Base side adjacent to } \angle A / \text{Perpendicular side opposite to } \angle A \dots (2)$$

On comparing equation (1) and (2), we get;

$$\text{Base side adjacent to } \angle A = 8$$

$$\text{Perpendicular side opposite to } \angle A = 15$$

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So, by using Pythagoras theorem to $\triangle ABC$, we have

$$AC^2 = AB^2 + BC^2$$

Substituting values for sides from the figure

$$AC^2 = 8^2 + 15^2$$

$$AC^2 = 64 + 225$$

$$AC^2 = 289$$

$$AC = \sqrt{289}$$

$$AC = 17$$

Therefore, hypotenuse = 17

By definition,

$\sin A = \text{Perpendicular/Hypotenuse}$

$$\Rightarrow \sin A = BC/AC$$

$\sin A = 15/17$ (using values from the above)

Also,

$$\sec A = 1/\cos A$$

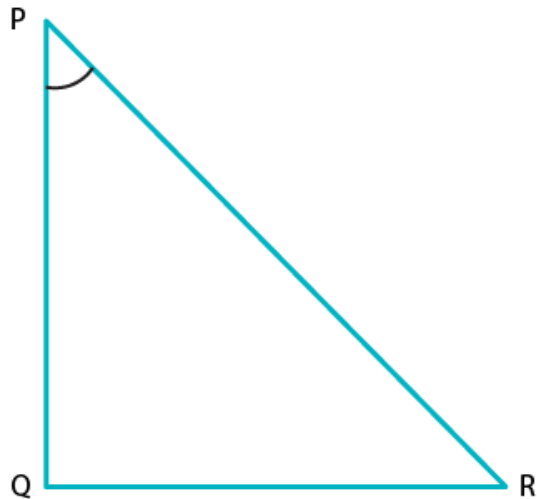
$$\Rightarrow \sec A = \text{Hypotenuse/ Base side adjacent to } \angle A$$

$$\therefore \sec A = 17/8$$

6. In $\triangle PQR$, right-angled at Q, PQ = 4cm and RQ = 3 cm. Find the value of $\sin P$, $\sin R$, $\sec P$ and $\sec R$.

Solution:

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Given:

$\triangle PQR$ is right-angled at Q.

$PQ = 4\text{cm}$

$RQ = 3\text{cm}$

Required to find: $\sin P$, $\sin R$, $\sec P$, $\sec R$

Given $\triangle PQR$,

By using Pythagoras theorem to $\triangle PQR$, we get

$$PR^2 = PQ^2 + RQ^2$$

Substituting the respective values,

$$PR^2 = 4^2 + 3^2$$

$$PR^2 = 16 + 9$$

$$PR^2 = 25$$

$$PR = \sqrt{25}$$

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$$PR = 5$$

$$\Rightarrow \text{Hypotenuse} = 5$$

By definition,

$\sin P = \frac{\text{Perpendicular side opposite to angle } P}{\text{Hypotenuse}}$

$$\sin P = \frac{RQ}{PR}$$

$$\Rightarrow \sin P = \frac{3}{5}$$

And,

$\sin R = \frac{\text{Perpendicular side opposite to angle } R}{\text{Hypotenuse}}$

$$\sin R = \frac{PQ}{PR}$$

$$\Rightarrow \sin R = \frac{4}{5}$$

And,

$$\sec P = \frac{1}{\cos P}$$

$\sec P = \frac{\text{Hypotenuse}}{\text{Base side adjacent to } \angle P}$

$$\sec P = \frac{PR}{PQ}$$

$$\Rightarrow \sec P = \frac{5}{4}$$

Now,

$$\sec R = \frac{1}{\cos R}$$

$\sec R = \frac{\text{Hypotenuse}}{\text{Base side adjacent to } \angle R}$

$$\sec R = \frac{PR}{RQ}$$

$$\Rightarrow \sec R = \frac{5}{3}$$

7. If $\cot \theta = \frac{7}{8}$, evaluate

(i) $\frac{(1+\sin \theta)(1-\sin \theta)}{(1+\cos \theta)(1-\cos \theta)}$

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(ii) $\cot^2 \theta$

Solution:

(i) Required to evaluate:

$$\frac{(1 + \sin\theta)(1 - \sin\theta)}{(1 + \cos\theta)(1 - \cos\theta)}$$

, given = $\cot \theta = 7/8$

Taking the numerator, we have

$$(1 + \sin \theta)(1 - \sin \theta) = 1 - \sin^2 \theta \text{ [Since, } (a+b)(a-b) = a^2 - b^2\text{]}$$

Similarly,

$$(1 + \cos \theta)(1 - \cos \theta) = 1 - \cos^2 \theta$$

We know that,

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\Rightarrow 1 - \cos^2 \theta = \sin^2 \theta$$

And,

$$1 - \sin^2 \theta = \cos^2 \theta$$

Thus,

$$(1 + \sin \theta)(1 - \sin \theta) = 1 - \sin^2 \theta = \cos^2 \theta$$

$$(1 + \cos \theta)(1 - \cos \theta) = 1 - \cos^2 \theta = \sin^2 \theta$$

\Rightarrow

$$\frac{(1 + \sin\theta)(1 - \sin\theta)}{(1 + \cos\theta)(1 - \cos\theta)}$$

$$= \cos^2 \theta / \sin^2 \theta$$

$$= (\cos \theta / \sin \theta)^2$$

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And, we know that $(\cos \theta / \sin \theta) = \cot \theta$

\Rightarrow

$$\frac{(1 + \sin \theta)(1 - \sin \theta)}{(1 + \cos \theta)(1 - \cos \theta)}$$

$$= (\cot \theta)^2$$

$$= (7/8)^2$$

$$= 49/64$$

(ii) Given,

$$\cot \theta = 7/8$$

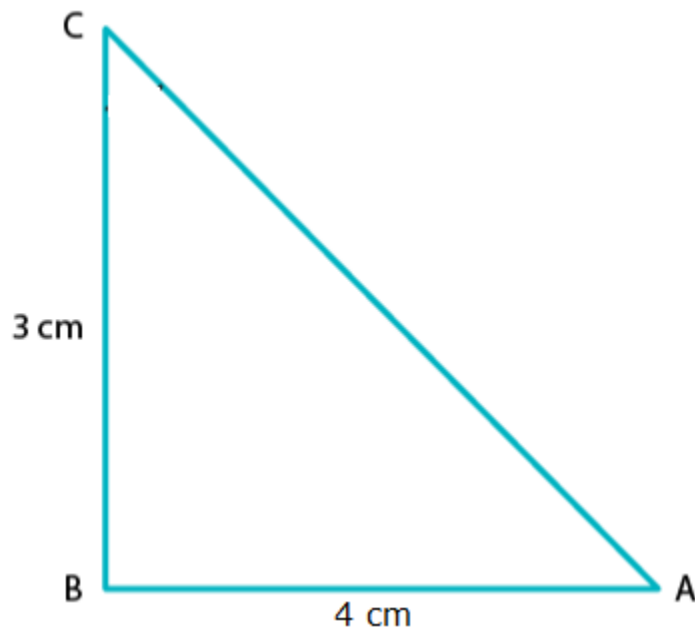
So, by squaring on both sides we get

$$(\cot \theta)^2 = (7/8)^2$$

$$\therefore \cot^2 \theta = 49/64$$

8. If $3 \cot A = 4$, check whether $(1 - \tan^2 A) / (1 + \tan^2 A) = (\cos^2 A - \sin^2 A)$ or not.

Solution:



Given,

$$3\cot A = 4$$

$$\Rightarrow \cot A = 4/3$$

By definition,

$$\tan A = 1/\cot A = 1/(4/3)$$

$$\Rightarrow \tan A = 3/4$$

Thus,

Base side adjacent to $\angle A = 4$

Perpendicular side opposite to $\angle A = 3$

In ΔABC , Hypotenuse is unknown

Thus, by applying Pythagoras theorem in ΔABC

We get

$$AC^2 = AB^2 + BC^2$$

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$$AC^2 = 4^2 + 3^2$$

$$AC^2 = 16 + 9$$

$$AC^2 = 25$$

$$AC = \sqrt{25}$$

$$AC = 5$$

Hence, hypotenuse = 5

Now, we can find that

$$\sin A = \frac{\text{opposite side to } \angle A}{\text{Hypotenuse}} = \frac{3}{5}$$

And,

$$\cos A = \frac{\text{adjacent side to } \angle A}{\text{Hypotenuse}} = \frac{4}{5}$$

Taking the LHS,

$$\text{Thus, LHS} = \frac{7}{25}$$

Now, taking RHS

$$\text{R.H.S} = \cos^2 A - \sin^2 A$$

Putting value of sin A and cos A

$$\text{R.H.S} = \left(\frac{4}{5}\right)^2 - \left(\frac{3}{5}\right)^2$$

$$\cos^2 A - \sin^2 A = \left(\frac{4}{5}\right)^2 - \left(\frac{3}{5}\right)^2$$

$$\cos^2 A - \sin^2 A = \frac{16}{25} - \frac{9}{25}$$

$$\cos^2 A - \sin^2 A = \frac{16-9}{25}$$

$$\cos^2 A - \sin^2 A = \frac{7}{25}$$

Therefore,

$$\frac{1 - \tan^2 A}{1 + \tan^2 A} = \cos^2 A - \sin^2 A$$

Hence Proved

9. If $\tan \theta = a/b$, find the value of $(\cos \theta + \sin \theta) / (\cos \theta - \sin \theta)$

Solution:

Given,

$$\tan \theta = a/b$$

And, we know by definition that

$$\tan \theta = \text{opposite side} / \text{adjacent side}$$

Thus, by comparison

$$\text{Opposite side} = a \text{ and adjacent side} = b$$

To find the hypotenuse, we know that by Pythagoras theorem that

$$\text{Hypotenuse}^2 = \text{opposite side}^2 + \text{adjacent side}^2$$

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$$\Rightarrow \text{Hypotenuse} = \sqrt{a^2 + b^2}$$

So, by definition

$\sin \theta = \text{opposite side} / \text{Hypotenuse}$

$$\sin \theta = a / \sqrt{a^2 + b^2}$$

And,

$\cos \theta = \text{adjacent side} / \text{Hypotenuse}$

$$\cos \theta = b / \sqrt{a^2 + b^2}$$

Now,

After substituting for $\cos \theta$ and $\sin \theta$, we have

$$\frac{\cos \theta + \sin \theta}{\cos \theta - \sin \theta} = \frac{(a + b) / \sqrt{a^2 + b^2}}{(a - b) / \sqrt{a^2 + b^2}} \quad \frac{\cos \theta + \sin \theta}{\cos \theta - \sin \theta} = \frac{(a + b)}{(a - b)}$$

\therefore

Hence Proved.

$$\frac{4 \cos \theta - \sin \theta}{2 \cos \theta + \sin \theta}$$

10. If $3 \tan \theta = 4$, find the value of

Solution:

Given, $3 \tan \theta = 4$

$$\Rightarrow \tan \theta = 4/3$$

$$\frac{4 \cos \theta - \sin \theta}{2 \cos \theta + \sin \theta}$$

From, let's divide the numerator and denominator by $\cos \theta$.

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We get,

$$(4 - \tan \theta) / (2 + \tan \theta)$$

$$\Rightarrow (4 - (4/3)) / (2 + (4/3)) \text{ [using the value of } \tan \theta \text{]}$$

$$\Rightarrow (12 - 4) / (6 + 4) \text{ [After taking LCM and cancelling it]}$$

$$\Rightarrow 8/10 = 4/5$$

$$\frac{4 \cos \theta - \sin \theta}{2 \cos \theta + \sin \theta}$$

$$\therefore = 4/5$$

$$\frac{4 \sin \theta - 3 \cos \theta}{2 \sin \theta + 6 \cos \theta}$$

11. If $3 \cot \theta = 2$, find the value of

Solution:

Given, $3 \cot \theta = 2$

$$\Rightarrow \cot \theta = 2/3$$

$$\frac{4 \sin \theta - 3 \cos \theta}{2 \sin \theta + 6 \cos \theta}$$

From, let's divide the numerator and denominator by $\sin \theta$.

We get,

$$(4 - 3 \cot \theta) / (2 + 6 \cot \theta)$$

$$\Rightarrow (4 - 3(2/3)) / (2 + 6(2/3)) \text{ [using the value of } \cot \theta \text{]}$$

$$\Rightarrow (4 - 2) / (2 + 4) \text{ [After taking LCM and simplifying it]}$$

$$\Rightarrow 2/6 = 1/3$$

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$$\frac{4 \sin \theta - 3 \cos \theta}{2 \sin \theta + 6 \cos \theta}$$

$$\therefore = 1/3$$

$$\frac{a \sin \theta - b \cos \theta}{a \sin \theta + b \cos \theta} = \frac{a^2 - b^2}{a^2 + b^2}$$

12. If $\tan \theta = a/b$, prove that

Solution:

Given, $\tan \theta = a/b$

$$\frac{a \sin \theta - b \cos \theta}{a \sin \theta + b \cos \theta}$$

From LHS, let's divide the numerator and denominator by $\cos \theta$.

And we get,

$$(a \tan \theta - b) / (a \tan \theta + b)$$

$$\Rightarrow (a(a/b) - b) / (a(a/b) + b) \text{ [using the value of } \tan \theta \text{]}$$

$$\Rightarrow (a^2 - b^2)/b^2 / (a^2 + b^2)/b^2 \text{ [After taking LCM and simplifying it]}$$

$$\Rightarrow (a^2 - b^2) / (a^2 + b^2)$$

= RHS

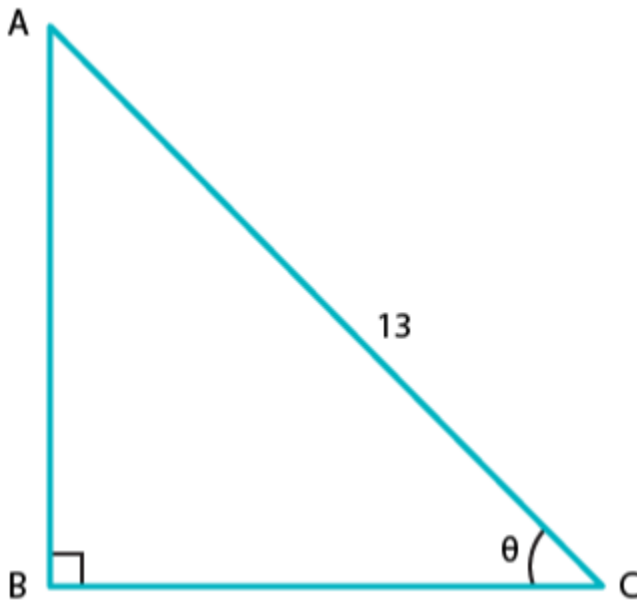
– Hence Proved

$$\frac{2 \sin \theta - 3 \cos \theta}{4 \sin \theta - 9 \cos \theta} = 3$$

13. If $\sec \theta = 13/5$, show that

Solution:

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Given,

$$\sec \theta = 13/5$$

We know that,

$$\sec \theta = 1 / \cos \theta$$

$$\Rightarrow \cos \theta = 1 / \sec \theta = 1 / (13/5)$$

$$\therefore \cos \theta = 5/13 \dots\dots (1)$$

By definition,

$$\cos \theta = \text{adjacent side} / \text{hypotenuse} \dots\dots (2)$$

Comparing (1) and (2), we have

Adjacent side = 5 and hypotenuse = 13

By Pythagoras theorem,

$$\text{Opposite side} = \sqrt{(\text{hypotenuse})^2 - (\text{adjacent side})^2}$$

$$= \sqrt{(13^2 - 5^2)}$$

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$$= \sqrt{169 - 25}$$

$$= \sqrt{144}$$

$$= 12$$

Thus, opposite side = 12

By definition,

$\tan \theta = \text{opposite side} / \text{adjacent side}$

$$\therefore \tan \theta = 12 / 5$$

$$\frac{2 \sin \theta - 3 \cos \theta}{4 \sin \theta - 9 \cos \theta}$$

From, let's divide the numerator and denominator by $\cos \theta$.

We get,

$$(2 \tan \theta - 3) / (4 \tan \theta - 9)$$

$$\Rightarrow (2(12/5) - 3) / (4(12/5) - 9) \text{ [using the value of } \tan \theta \text{]}$$

$$\Rightarrow (24 - 15) / (48 - 45) \text{ [After taking LCM and cancelling it]}$$

$$\Rightarrow 9/3 = 3$$

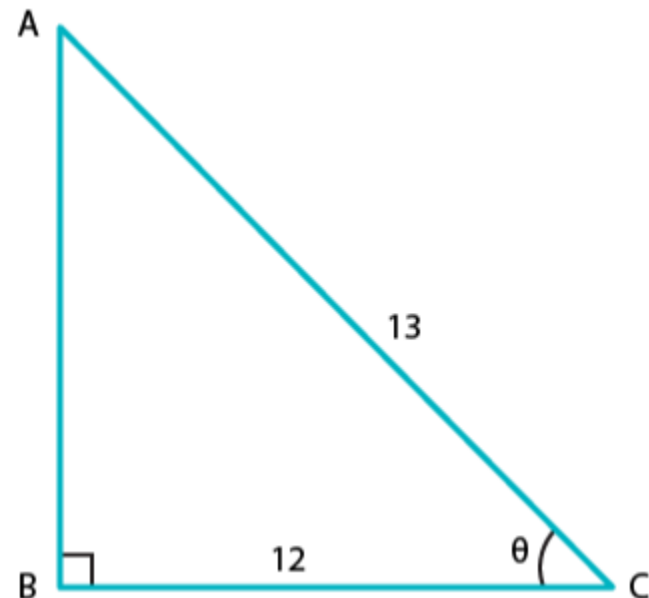
$$\frac{2 \sin \theta - 3 \cos \theta}{4 \sin \theta - 9 \cos \theta}$$

$$\therefore = 3$$

14. If $\cos \theta = 12/13$, show that $\sin \theta(1 - \tan \theta) = 35/156$

Solution:

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Given, $\cos \theta = 12/13$ (1)

By definition we know that,

$\cos \theta = \text{Base side adjacent to } \angle \theta / \text{Hypotenuse}$ (2)

When comparing equation (1) and (2), we get

Base side adjacent to $\angle \theta = 12$ and Hypotenuse = 13

From the figure,

Base side BC = 12

Hypotenuse AC = 13

Side AB is unknown here and it can be found by using Pythagoras theorem

Thus by applying Pythagoras theorem,

$$AC^2 = AB^2 + BC^2$$

$$13^2 = AB^2 + 12^2$$

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Therefore,

$$AB^2 = 13^2 - 12^2$$

$$AB^2 = 169 - 144$$

$$AB^2 = 25$$

$$AB = \sqrt{25}$$

$$AB = 5 \dots (3)$$

Now, we know that

$\sin \theta = \text{Perpendicular side opposite to } \angle \theta / \text{Hypotenuse}$

Thus, $\sin \theta = AB/AC$ [from figure]

$$\Rightarrow \sin \theta = 5/13 \dots (4)$$

$$\text{And, } \tan \theta = \sin \theta / \cos \theta = (5/13) / (12/13)$$

$$\Rightarrow \tan \theta = 12/13 \dots (5)$$

Taking L.H.S we have

$$\text{L.H.S} = \sin \theta (1 - \tan \theta)$$

Substituting the value of $\sin \theta$ and $\tan \theta$ from equation (4) and (5)

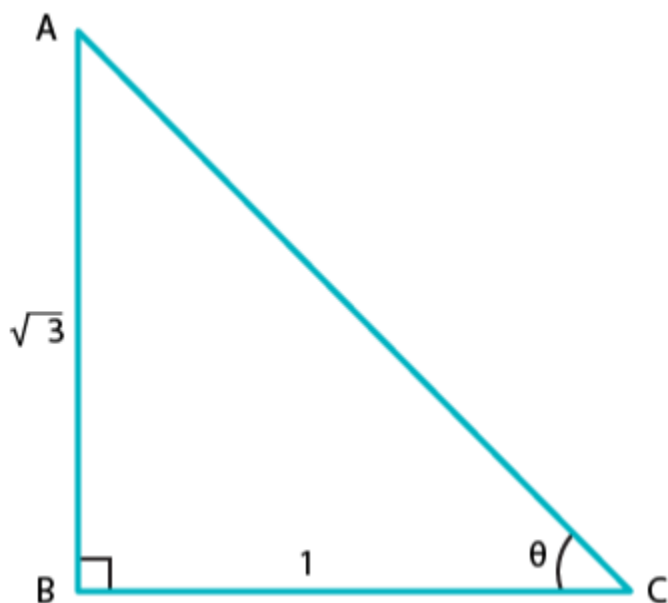
We get,

$$\text{If } \cot \theta = \frac{1}{\sqrt{3}}, \text{ show that } \frac{1 - \cos^2 \theta}{2 - \sin^2 \theta} = \frac{3}{5}$$

15.

Solution:

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Given, $\cot \theta = 1/\sqrt{3}$ (1)

By definition we know that,

$$\cot \theta = 1/\tan \theta$$

And, since $\tan \theta = \text{perpendicular side opposite to } \angle \theta / \text{Base side adjacent to } \angle \theta$

$\Rightarrow \cot \theta = \text{Base side adjacent to } \angle \theta / \text{perpendicular side opposite to } \angle \theta$ (2)[Since they are reciprocal to each other]

On comparing equation (1) and (2), we get

Base side adjacent to $\angle \theta = 1$ and Perpendicular side opposite to $\angle \theta = \sqrt{3}$

Therefore, the triangle formed is,

On substituting the values of known sides as $AB = \sqrt{3}$ and $BC = 1$

$$AC^2 = (\sqrt{3})^2 + 1$$

$$AC^2 = 3 + 1$$

$$AC^2 = 4$$

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$$AC = \sqrt{4}$$

$$\text{Therefore, } AC = 2 \dots (3)$$

Now, by definition

$$\sin \theta = \text{Perpendicular side opposite to } \angle \theta / \text{Hypotenuse} = AB / AC$$

$$\Rightarrow \sin \theta = \sqrt{3} / 2 \dots\dots(4)$$

$$\text{And, } \cos \theta = \text{Base side adjacent to } \angle \theta / \text{Hypotenuse} = BC / AC$$

$$\Rightarrow \cos \theta = 1 / 2 \dots\dots (5)$$

Now, taking L.H.S we have

$$\text{L. H. S} = \frac{1 - \cos^2 \theta}{2 - \sin^2 \theta}$$

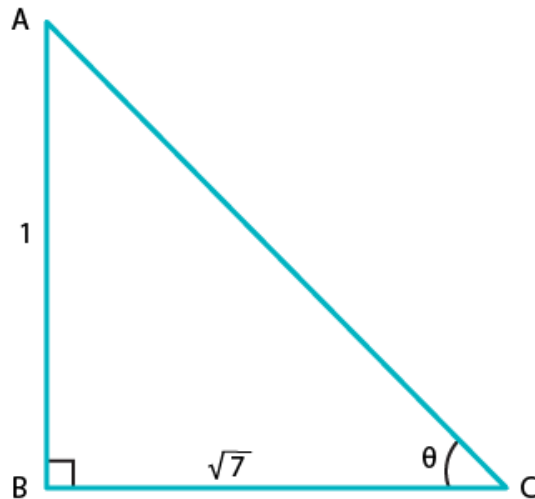
Substituting the values from equation (4) and (5), we have

$$\text{If } \tan \theta = \frac{1}{\sqrt{7}}, \text{ then show that } \frac{\operatorname{cosec}^2 \theta - \sec^2 \theta}{\operatorname{cosec}^2 \theta + \sec^2 \theta} = \frac{3}{4}$$

16.

Solution:

$$\text{Given, } \tan \theta = 1 / \sqrt{7} \dots\dots(1)$$



By definition, we know that

$$\tan \theta = \text{Perpendicular side opposite to } \angle \theta / \text{Base side adjacent to } \angle \theta \dots\dots(2)$$

On comparing equation (1) and (2), we have

$$\text{Perpendicular side opposite to } \angle \theta = 1$$

$$\text{Base side adjacent to } \angle \theta = \sqrt{7}$$

Thus, the triangle representing $\angle \theta$ is,

Hypotenuse AC is unknown and it can be found by using Pythagoras theorem

By applying Pythagoras theorem, we have

$$AC^2 = AB^2 + BC^2$$

$$AC^2 = 1^2 + (\sqrt{7})^2$$

$$AC^2 = 1 + 7$$

$$AC^2 = 8$$

$$AC = \sqrt{8}$$

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$$\Rightarrow AC = 2\sqrt{2}$$

By definition,

$$\sin \theta = \text{Perpendicular side opposite to } \angle \theta / \text{Hypotenuse} = AB / AC$$

$$\Rightarrow \sin \theta = 1 / 2\sqrt{2}$$

And, since $\operatorname{cosec} \theta = 1/\sin \theta$

$$\Rightarrow \operatorname{cosec} \theta = 2\sqrt{2} \dots\dots\dots (3)$$

Now,

$$\cos \theta = \text{Base side adjacent to } \angle \theta / \text{Hypotenuse} = BC / AC$$

$$\Rightarrow \cos \theta = \sqrt{7} / 2\sqrt{2}$$

And, since $\sec \theta = 1 / \sin \theta$

$$\Rightarrow \sec \theta = 2\sqrt{2} / \sqrt{7} \dots\dots\dots (4)$$

Taking the L.H.S of the equation,

$$\text{L. H. S} = \frac{\operatorname{cosec}^2 \theta - \sec^2 \theta}{\operatorname{cosec}^2 \theta + \sec^2 \theta}$$

Substituting the value of $\operatorname{cosec} \theta$ and $\sec \theta$ from equation (3) and (4), we get

$$\frac{\sin \theta - 2\cos \theta}{\tan \theta - \cot \theta}$$

17. If $\sec \theta = 5/4$, find the value of

Solution:

Given,

$$\sec \theta = 5/4$$

We know that,

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$$\sec \theta = 1 / \cos \theta$$

$$\Rightarrow \cos \theta = 1 / (5/4) = 4/5 \dots\dots (1)$$

By definition,

$$\cos \theta = \text{Base side adjacent to } \angle \theta / \text{Hypotenuse} \dots (2)$$

On comparing equation (1) and (2), we have

$$\text{Hypotenuse} = 5$$

$$\text{Base side adjacent to } \angle \theta = 4$$

Thus, the triangle representing $\angle \theta$ is ABC.

Perpendicular side opposite to $\angle \theta$, AB is unknown and it can be found by using Pythagoras theorem

By applying Pythagoras theorem, we have

$$AC^2 = AB^2 + BC^2$$

$$AB^2 = AC^2 - BC^2$$

$$AB^2 = 5^2 - 4^2$$

$$AB^2 = 25 - 16$$

$$AB = \sqrt{9}$$

$$\Rightarrow AB = 3$$

By definition,

$$\sin \theta = \text{Perpendicular side opposite to } \angle \theta / \text{Hypotenuse} = AB / AC$$

$$\Rightarrow \sin \theta = 3/5 \dots\dots(3)$$

Now, $\tan \theta = \text{Perpendicular side opposite to } \angle \theta / \text{Base side adjacent to } \angle \theta$

$$\Rightarrow \tan \theta = 3/4 \dots\dots(4)$$

And, since $\cot \theta = 1 / \tan \theta$

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$$\Rightarrow \cot \theta = 4/3 \dots\dots(5)$$

Now,

Substituting the value of $\sin \theta$, $\cos \theta$, $\cot \theta$ and $\tan \theta$ from the equations (1), (3), (4) and (5) we have,

$$\frac{\sin \theta - 2 \cos \theta}{\tan \theta - \cot \theta} = \frac{\frac{3}{5} - 2\left(\frac{4}{5}\right)}{\frac{3}{4} - \frac{4}{3}}$$

$$= 12/7$$

Therefore,

$$\frac{\sin \theta - 2 \cos \theta}{\tan \theta - \cot \theta} = \frac{12}{7} \frac{2 \sin \theta \cos \theta}{\cos^2 \theta - \sin^2 \theta}$$

18. If $\tan \theta = 12/13$, find the value of

Solution:

Given,

$$\tan \theta = 12/13 \dots\dots\dots (1)$$

We know that by definition,

$$\tan \theta = \text{Perpendicular side opposite to } \angle \theta / \text{Base side adjacent to } \angle \theta \dots\dots (2)$$

On comparing equation (1) and (2), we have

$$\text{Perpendicular side opposite to } \angle \theta = 12$$

$$\text{Base side adjacent to } \angle \theta = 13$$

Thus, in the triangle representing $\angle \theta$ we have,

Hypotenuse AC is the unknown and it can be found by using Pythagoras theorem

So by applying Pythagoras theorem, we have

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$$AC^2 = 12^2 + 13^2$$

$$AC^2 = 144 + 169$$

$$AC^2 = 313$$

$$\Rightarrow AC = \sqrt{313}$$

By definition,

$\sin \theta = \frac{\text{Perpendicular side opposite to } \angle \theta}{\text{Hypotenuse}} = \frac{AB}{AC}$

$$\Rightarrow \sin \theta = \frac{12}{\sqrt{313}} \dots (3)$$

And, $\cos \theta = \frac{\text{Base side adjacent to } \angle \theta}{\text{Hypotenuse}} = \frac{BC}{AC}$

$$\Rightarrow \cos \theta = \frac{13}{\sqrt{313}} \dots (4)$$

Now, substituting the value of $\sin \theta$ and $\cos \theta$ from equation (3) and (4) respectively in the equation below

$$\frac{2 \sin \theta \cos \theta}{\cos^2 \theta - \sin^2 \theta} = \frac{2 \times \frac{13}{\sqrt{313}} \times \frac{12}{\sqrt{313}}}{\left(\frac{13}{\sqrt{313}}\right)^2 - \left(\frac{12}{\sqrt{313}}\right)^2}$$

$$= \frac{312}{\frac{313}{25}}$$

$$= \frac{312}{25}$$

Therefore,

$$\frac{2 \sin \theta \cos \theta}{\cos^2 \theta - \sin^2 \theta} = \frac{312}{25}$$

Exercise 5.2 Page No: 5.41

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Evaluate each of the following:

1. $\sin 45^\circ \sin 30^\circ + \cos 45^\circ \cos 30^\circ$

Solution:

$$\sin 45^\circ \sin 30^\circ + \cos 45^\circ \cos 30^\circ$$

Value of trigonometric ratios are:

$$\sin 45^\circ = \frac{1}{\sqrt{2}} \quad \sin 30^\circ = \frac{1}{2}$$

$$\cos 45^\circ = \frac{1}{\sqrt{2}} \quad \cos 30^\circ = \frac{\sqrt{3}}{2}$$

Substituting in the given equation, we get

$$\frac{1}{\sqrt{2}} \cdot \frac{1}{2} + \frac{1}{\sqrt{2}} \cdot \frac{\sqrt{3}}{2}$$

$$= \frac{1}{\sqrt{2}} \cdot \frac{\sqrt{3}}{2\sqrt{2}}$$

$$= \frac{\sqrt{3}+1}{2\sqrt{2}}$$

2. $\sin 60^\circ \cos 30^\circ + \cos 60^\circ \sin 30^\circ$

Solution:

$$\sin 60^\circ \cos 30^\circ + \cos 60^\circ \sin 30^\circ$$

By trigonometric ratios we have ,

$$\sin 60^\circ = \frac{\sqrt{3}}{2} \quad \sin 30^\circ = \frac{1}{2}$$

$$\cos 30^\circ = \frac{\sqrt{3}}{2} \quad \cos 60^\circ = \frac{1}{2}$$

Substituting the values in given equation

$$= \frac{\sqrt{3}}{2} \cdot \frac{\sqrt{3}}{2} + \frac{1}{2} \cdot \frac{1}{2}$$

$$= \frac{3}{4} + \frac{1}{4} = \frac{4}{4} = 1$$

3. $\cos 60^\circ \cos 45^\circ - \sin 60^\circ \sin 45^\circ$

Solution:

$$\cos 60^\circ \cos 45^\circ - \sin 60^\circ \sin 45^\circ$$

We know that by trigonometric ratios

$$\cos 60^\circ = \frac{1}{2} \quad \cos 45^\circ = \frac{1}{\sqrt{2}}$$

$$\sin 60^\circ = \frac{\sqrt{3}}{2} \quad \sin 45^\circ = \frac{1}{\sqrt{2}}$$

Substituting the values in given equation

$$\frac{1}{2} \cdot \frac{1}{\sqrt{2}} - \frac{\sqrt{3}}{2} \cdot \frac{1}{\sqrt{2}}$$

$$= \frac{1-\sqrt{3}}{2\sqrt{2}}$$

4. $\sin^2 30^\circ + \sin^2 45^\circ + \sin^2 60^\circ + \sin^2 90^\circ$

Solution:

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$$\sin^2 30^\circ + \sin^2 45^\circ + \sin^2 60^\circ + \sin^2 90^\circ$$

We know that by trigonometric ratios

$$\sin 30^\circ = \frac{1}{2} \quad \sin 45^\circ = \frac{1}{\sqrt{2}}$$

$$\sin 60^\circ = \frac{\sqrt{3}}{2} \quad \sin 90^\circ = 1$$

Substituting the values in given equation, we get

$$\begin{aligned} &= \left[\frac{1}{2}\right]^2 + \left[\frac{1}{\sqrt{2}}\right]^2 + \left[\frac{\sqrt{3}}{2}\right]^2 + 1 \\ &= \frac{1}{4} + \frac{1}{2} + \frac{3}{4} + 1 \\ &= \frac{5}{2} \end{aligned}$$

5. $\cos^2 30^\circ + \cos^2 45^\circ + \cos^2 60^\circ + \cos^2 90^\circ$

Solution:

$$\cos^2 30^\circ + \cos^2 45^\circ + \cos^2 60^\circ + \cos^2 90^\circ$$

We know that by trigonometric ratios

$$\cos 30^\circ = \frac{\sqrt{3}}{2} \quad \cos 45^\circ = \frac{1}{\sqrt{2}}$$

$$\cos 60^\circ = \frac{1}{2} \quad \cos 90^\circ = 0$$

Substituting the values in given equation

$$\begin{aligned} & \left[\frac{\sqrt{3}}{2} \right]^2 + \left[\frac{1}{\sqrt{2}} \right]^2 + \left[\frac{1}{2} \right]^2 + 0 \\ &= \frac{3}{4} + \frac{1}{2} + \frac{1}{4} \\ &= \frac{3}{2} \end{aligned}$$

6. $\tan^2 30^\circ + \tan^2 45^\circ + \tan^2 60^\circ$

Solution:

$$\tan^2 30^\circ + \tan^2 45^\circ + \tan^2 60^\circ$$

We know that by trigonometric ratios

$$\tan 30^\circ = \frac{1}{\sqrt{3}} \quad \tan 60^\circ = \sqrt{3}$$

$$\tan 45^\circ = 1$$

Substituting the values in given equation

$$\begin{aligned} & \left[\frac{1}{\sqrt{3}} \right]^2 + [\sqrt{3}]^2 + 1 \\ &= \frac{1}{3} + 3 + 1 \\ &= \frac{13}{3} \end{aligned}$$

7. $2\sin^2 30^\circ - 3\cos^2 45^\circ + \tan^2 60^\circ$

Solution:

$$2\sin^2 30^\circ - 3\cos^2 45^\circ + \tan^2 60^\circ$$

We know that by trigonometric ratios

$$\sin 30^\circ = \frac{1}{2} \quad \cos 45^\circ = \frac{1}{\sqrt{2}}$$

$$\tan 60^\circ = \sqrt{3}$$

Substituting the values in given equation

$$= 2\left(\frac{1}{2}\right)^2 - 3\left(\frac{1}{\sqrt{2}}\right)^2 + (\sqrt{3})^2$$

$$= 2\left(\frac{1}{4}\right) - 3\left(\frac{1}{2}\right) + 3$$

$$= \frac{1-3+6}{2}$$

$$= 2$$

8. $\sin^2 30^\circ \cos^2 45^\circ + 4\tan^2 30^\circ + (1/2) \sin^2 90^\circ - 2\cos^2 90^\circ + (1/24) \cos 20^\circ$

Solution:

$$\sin^2 30^\circ \cos^2 45^\circ + 4\tan^2 30^\circ + \frac{1}{2}\sin^2 90^\circ - 2\cos^2 90^\circ + \frac{1}{24}\cos^2 0^\circ$$

We know that by trigonometric ratios

$$\sin 30^\circ = \frac{1}{2}$$

$$\cos 45^\circ = \frac{1}{\sqrt{2}}$$

$$\tan 30^\circ = \frac{1}{\sqrt{3}}$$

$$\sin 90^\circ = 1$$

$$\cos 90^\circ = 0$$

$$\cos 0^\circ = 1$$

Substituting the values in given equation

$$\begin{aligned} & \left[\frac{1}{2}\right]^2 \cdot \left[\frac{1}{\sqrt{2}}\right]^2 + 4\left[\frac{1}{\sqrt{3}}\right]^2 + \frac{1}{2}[1]^2 - 2[0]^2 + \frac{1}{24}[1]^2 \\ &= \frac{1}{8} + \frac{4}{3} + \frac{1}{2} + \frac{1}{24} \\ &= \frac{48}{24} \\ &= 2 \end{aligned}$$

$$\sin^2 30^\circ \cos^2 45^\circ + 4\tan^2 30^\circ + \frac{1}{2}\sin^2 90^\circ - 2\cos^2 90^\circ + \frac{1}{24}\cos^2 0^\circ$$

We know that by trigonometric ratios

$$\sin 30^\circ = \frac{1}{2}$$

$$\cos 45^\circ = \frac{1}{\sqrt{2}}$$

$$\tan 30^\circ = \frac{1}{\sqrt{3}}$$

$$\sin 90^\circ = 1$$

$$\cos 90^\circ = 0$$

$$\cos 0^\circ = 1$$

Substituting the values in given equation

$$\begin{aligned} & \left[\frac{1}{2}\right]^2 \cdot \left[\frac{1}{\sqrt{2}}\right]^2 + 4\left[\frac{1}{\sqrt{3}}\right]^2 + \frac{1}{2}[1]^2 - 2[0]^2 + \frac{1}{24}[1]^2 \\ &= \frac{1}{8} + \frac{4}{3} + \frac{1}{2} + \frac{1}{24} \\ &= \frac{48}{24} \\ &= 2 \end{aligned}$$

9. $4(\sin^4 60^\circ + \cos^4 30^\circ) - 3(\tan^2 60^\circ - \tan^2 45^\circ) + 5\cos^2 45^\circ$

Solution:

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$$4 (\sin^4 60^\circ + \cos^4 30^\circ) - 3 (\tan^2 60^\circ - \tan^2 45^\circ) + 5 \cos^2 45^\circ$$

We know that by trigonometric ratios we have ,

$$\sin 60^\circ = \frac{\sqrt{3}}{2} \quad \cos 45^\circ = \frac{1}{\sqrt{2}}$$

$$\tan 60^\circ = \sqrt{3} \quad \cos 30^\circ = \frac{\sqrt{3}}{2}$$

Substituting the values in given equation

$$= 4 \cdot \frac{18}{16} - 6 + \frac{5}{2}$$

$$= \frac{1}{4} - 6 + \frac{5}{2}$$

$$= \frac{14}{2} - 6 = 7 - 6 = 1$$

10. $(\operatorname{cosec}^2 45^\circ \sec^2 30^\circ)(\sin^2 30^\circ + 4\cot^2 45^\circ - \sec^2 60^\circ)$

Solution:

$$(\operatorname{cosec}^2 45^\circ \sec^2 30^\circ) (\sin^2 30^\circ + 4\cot^2 45^\circ - \sec^2 60^\circ)$$

We know that by trigonometric ratios,

$$\operatorname{cosec} 45^\circ = \sqrt{2} \sec 30^\circ = \frac{2}{\sqrt{3}}$$

$$\sin 30^\circ = \frac{1}{2} \cot 45^\circ = 1$$

$$\sec 60^\circ = 2$$

Substituting the values in given equation

$$\begin{aligned} & \left([\sqrt{2}]^2 \cdot \left[\frac{2}{\sqrt{3}} \right]^2 \right) \left(\left[\frac{1}{2} \right]^2 + 4(1) - (2)^2 \right) \\ &= (2 \cdot (4/3)) [(1/4) + 4 - 4] = (8/3) \cdot (1/4) \\ &= \frac{2}{3} \end{aligned}$$

11. $\operatorname{cosec}^3 30^\circ \cos 60^\circ \tan^3 45^\circ \sin^2 90^\circ \sec^2 45^\circ \cot 30^\circ$

Solution:

$$\operatorname{cosec}^3 30^\circ \cos 60^\circ \tan^3 45^\circ \sin^2 90^\circ \sec^2 45^\circ \cot 30^\circ$$

Using trigonometric values, we have

$$= (2)^3 \times \left(\frac{1}{2}\right) \times (1^3) \times (1^2) \times (\sqrt{2}^2) \times (\sqrt{3})$$

$$= 8 \times \left(\frac{1}{2}\right) \times (1) \times (1) \times (2) \times (\sqrt{3})$$

$$= 8\sqrt{3}$$

12. $\cot^2 30^\circ - 2\cos^2 60^\circ - (3/4)\sec^2 45^\circ - 4\sec^2 30^\circ$

Solution:

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Using trigonometric values, we have

$$\begin{aligned} & \cot^2 30^\circ - 2\cos^2 60^\circ - \frac{3}{4}\sec^2 45^\circ - 4\sec^2 30^\circ \\ &= (\sqrt{3}^2) - 2\left(\frac{1}{2}\right)^2 - \left(\frac{3}{4} \times \sqrt{2}^2\right) - \left(4 \times \left(\frac{2}{\sqrt{3}}\right)^2\right) \\ &= 3 - \frac{1}{2} - \frac{3}{2} - \frac{16}{3} \\ &= \frac{-13}{3} \end{aligned}$$

13. $(\cos 0^\circ + \sin 45^\circ + \sin 30^\circ)(\sin 90^\circ - \cos 45^\circ + \cos 60^\circ)$

Solution:

$$(\cos 0^\circ + \sin 45^\circ + \sin 30^\circ)(\sin 90^\circ - \cos 45^\circ + \cos 60^\circ)$$

Using trigonometric values, we have

$$\begin{aligned} &= \left(1 + \frac{1}{\sqrt{2}} + \frac{1}{2}\right) \left(1 - \frac{1}{\sqrt{2}} + \frac{1}{2}\right) \\ &= \left(\frac{3}{2} + \frac{1}{\sqrt{2}}\right) \left(\frac{3}{2} - \frac{1}{\sqrt{2}}\right) \\ &= \left(\left(\frac{3}{2}\right)^2 - \left(\frac{1}{\sqrt{2}}\right)^2\right) \\ &= \frac{9}{4} - \frac{1}{2} \\ &= \frac{7}{4} \end{aligned}$$

$$\frac{\sin 30^\circ - \sin 90^\circ + 2 \cos 0^\circ}{\tan 30^\circ \tan 60^\circ}$$

14.

Solution:

Given,

$$\frac{\sin 30^\circ - \sin 90^\circ + 2 \cos 0^\circ}{\tan 30^\circ \tan 60^\circ}$$

Using trigonometric values, we have

$$\begin{aligned} &= \frac{\frac{1}{2} - 1 + 2}{\frac{1}{\sqrt{3}} \times \sqrt{3}} \\ &= \frac{3}{2} \end{aligned}$$

15. $4/\cot^2 30^\circ + 1/\sin^2 60^\circ - \cos^2 45^\circ$

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Solution:

$$\begin{aligned} & \frac{4}{\cot^2 30^\circ} + \frac{1}{\sin^2 60^\circ} - \cos^2 45^\circ \\ &= \frac{4}{(\sqrt{3})^2} + \frac{1}{\left(\frac{\sqrt{3}}{2}\right)^2} - \left(\frac{1}{\sqrt{2}}\right)^2 \\ &= \frac{4}{3} + \frac{4}{3} - \frac{1}{2} \\ &= \frac{16-3}{6} \\ &= \frac{13}{6} \end{aligned}$$

16. $4(\sin^4 30^\circ + \cos^2 60^\circ) - 3(\cos^2 45^\circ - \sin^2 90^\circ) - \sin^2 60^\circ$

Solution:

Using trigonometric values, we have

$$\begin{aligned} & 4(\sin^4 30^\circ + \cos^2 60^\circ) - 3(\cos^2 45^\circ - \sin^2 90^\circ) - \sin^2 60^\circ \\ &= 4\left(\left(\frac{1}{2}\right)^4 + \left(\frac{1}{2}\right)^2\right) - 3\left(\left(\frac{1}{\sqrt{2}}\right)^2 - 1\right) - \left(\frac{\sqrt{3}}{2}\right)^2 \\ &= 4\left(\frac{1}{16} + \frac{1}{4}\right) + \frac{3}{2} - \frac{3}{4} \\ &= \frac{8}{4} = 2 \end{aligned}$$

$$\frac{\tan^2 60^\circ + 4\cos^2 45^\circ + 3\sec^2 30^\circ + 5\cos^2 90^\circ}{\operatorname{cosec} 30^\circ + \sec 60^\circ - \cot^2 30^\circ}$$

17.

Solution:

Using trigonometric values, we have

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$$\frac{\tan^2 60^\circ + 4\cos^2 45^\circ + 3\sec^2 30^\circ + 5\cos^2 90^\circ}{\operatorname{cosec} 30^\circ + \sec 60^\circ - \cot^2 30^\circ}$$

$$= \frac{(\sqrt{3})^2 + 4\left(\frac{1}{\sqrt{2}}\right)^2 + 3\left(\frac{2}{\sqrt{3}}\right)^2 + 5(0)}{2 + 2 - (\sqrt{3})^2}$$

$$= 3 + 2 + 4$$

$$= 9$$

$$\frac{\sin 30^\circ}{\sin 45^\circ} + \frac{\tan 45^\circ}{\sec 60^\circ} - \frac{\sin 60^\circ}{\cot 45^\circ} - \frac{\cos 30^\circ}{\sin 90^\circ}$$

18.

Solution:

Using trigonometric values, we have

$$\frac{\sin 30^\circ}{\sin 45^\circ} + \frac{\tan 45^\circ}{\sec 60^\circ} - \frac{\sin 60^\circ}{\cot 45^\circ} - \frac{\cos 30^\circ}{\sin 90^\circ}$$

$$= \frac{\frac{1}{2}}{\frac{1}{\sqrt{2}}} + \frac{1}{2} - \frac{\frac{\sqrt{3}}{2}}{1} - \frac{\frac{\sqrt{3}}{2}}{1}$$

$$= \frac{\sqrt{2}}{2} + \frac{1}{2} - \frac{\sqrt{3}}{2} - \frac{\sqrt{3}}{2}$$

$$= \frac{\sqrt{2} + 1 - 2\sqrt{3}}{2}$$

$$\frac{\tan 45^\circ}{\operatorname{cosec} 30^\circ} + \frac{\sec 60^\circ}{\cot 45^\circ} - \frac{5\sin 90^\circ}{2\cos 0^\circ}$$

19.

Solution:

Using trigonometric values, we have

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$$\frac{\tan 45^\circ}{\operatorname{cosec} 30^\circ} + \frac{\sec 60^\circ}{\cot 45^\circ} - \frac{5 \sin 90^\circ}{2 \cos 0^\circ}$$

$$= \frac{1}{2} + \frac{2}{1} - \frac{5(1)}{2(1)}$$

$$= \frac{5}{2} - \frac{5}{2}$$

$$= 0$$

Find the value of x in each of the following: (20-25)

20. $2 \sin 3x = \sqrt{3}$

Solution:

Given,

$$2 \sin 3x = \sqrt{3}$$

$$\sin 3x = \sqrt{3}/2$$

$$\sin 3x = \sin 60^\circ$$

$$3x = 60^\circ$$

$$x = 20^\circ$$

Exercise 5.3 Page No: 5.52

1. Evaluate the following:

(i) $\sin 20^\circ / \cos 70^\circ$

(ii) $\cos 19^\circ / \sin 71^\circ$

(iii) $\sin 21^\circ / \cos 69^\circ$

(iv) $\tan 10^\circ / \cot 80^\circ$

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(v) $\sec 11^\circ / \operatorname{cosec} 79^\circ$

Solution:

(i) We have,

$$\sin 20^\circ / \cos 70^\circ = \sin (90^\circ - 70^\circ) / \cos 70^\circ = \cos 70^\circ / \cos 70^\circ = 1 \quad [\because \sin (90 - \theta) = \cos \theta]$$

(ii) We have,

$$\cos 19^\circ / \sin 71^\circ = \cos (90^\circ - 71^\circ) / \sin 71^\circ = \sin 71^\circ / \sin 71^\circ = 1 \quad [\because \cos (90 - \theta) = \sin \theta]$$

(iii) We have,

$$\sin 21^\circ / \cos 69^\circ = \sin (90^\circ - 69^\circ) / \cos 69^\circ = \cos 69^\circ / \cos 69^\circ = 1 \quad [\because \sin (90 - \theta) = \cos \theta]$$

(iv) We have,

$$\tan 10^\circ / \cot 80^\circ = \tan (90^\circ - 10^\circ) / \cot 80^\circ = \cot 80^\circ / \cot 80^\circ = 1 \quad [\because \tan (90 - \theta) = \cot \theta]$$

(v) We have,

$$\sec 11^\circ / \operatorname{cosec} 79^\circ = \sec (90^\circ - 79^\circ) / \operatorname{cosec} 79^\circ = \operatorname{cosec} 79^\circ / \operatorname{cosec} 79^\circ = 1 \quad [\because \sec (90 - \theta) = \operatorname{cosec} \theta]$$

2. Evaluate the following:

(i) $\left(\frac{\sin 49^\circ}{\cos 41^\circ}\right)^2 + \left(\frac{\cos 41^\circ}{\sin 49^\circ}\right)^2$

Solution:

We have, $[\because \sin (90 - \theta) = \cos \theta$ and $\cos (90 - \theta) = \sin \theta]$

$$\begin{aligned} & \left(\frac{\sin 49^\circ}{\cos 41^\circ}\right)^2 + \left(\frac{\cos 41^\circ}{\sin 49^\circ}\right)^2 \\ &= \left(\frac{\sin(90^\circ - 41^\circ)}{\cos 41^\circ}\right)^2 + \left(\frac{\cos(90^\circ - 49^\circ)}{\sin 49^\circ}\right)^2 \\ &= \left(\frac{\cos 41^\circ}{\cos 41^\circ}\right)^2 + \left(\frac{\sin 49^\circ}{\sin 49^\circ}\right)^2 \end{aligned}$$

$$= 1^2 + 1^2 = 1 + 1$$

$$= 2$$

(ii) $\cos 48^\circ - \sin 42^\circ$

Solution:

We know that, $\cos(90^\circ - \theta) = \sin \theta$.

So,

$$\cos 48^\circ - \sin 42^\circ = \cos(90^\circ - 42^\circ) - \sin 42^\circ = \sin 42^\circ - \sin 42^\circ = 0$$

Thus the value of $\cos 48^\circ - \sin 42^\circ$ is 0.

(iii) $\frac{\cot 40^\circ}{\tan 50^\circ} - \frac{1}{2} \left(\frac{\cos 35^\circ}{\sin 55^\circ}\right)$

Solution:

We have, [$\because \cot(90 - \theta) = \tan \theta$ and $\cos(90 - \theta) = \sin \theta$]

$$\begin{aligned} & \frac{\cot 40^\circ}{\tan 50^\circ} - \frac{1}{2} \left(\frac{\cos 35^\circ}{\sin 55^\circ} \right) \\ &= \frac{\cot(90^\circ - 50^\circ)}{\tan 50^\circ} - \frac{1}{2} \left(\frac{\cos(90^\circ - 55^\circ)}{\sin 55^\circ} \right) \\ &= \frac{\tan 50^\circ}{\tan 50^\circ} - \frac{1}{2} \left(\frac{\sin 55^\circ}{\sin 55^\circ} \right) \end{aligned}$$

$$= 1 - 1/2(1)$$

$$= 1/2$$

$$(iv) \left(\frac{\sin 27^\circ}{\cos 63^\circ} \right)^2 - \left(\frac{\cos 63^\circ}{\sin 27^\circ} \right)^2$$

Solution:

We have, [$\because \sin(90 - \theta) = \cos \theta$ and $\cos(90 - \theta) = \sin \theta$]

$$\begin{aligned} & \left(\frac{\sin 27^\circ}{\cos 63^\circ} \right)^2 - \left(\frac{\cos 63^\circ}{\sin 27^\circ} \right)^2 \\ &= \left(\frac{\sin(90^\circ - 63^\circ)}{\cos 63^\circ} \right)^2 - \left(\frac{\cos(90^\circ - 27^\circ)}{\sin 27^\circ} \right)^2 \\ &= \left(\frac{\cos 63^\circ}{\cos 63^\circ} \right)^2 - \left(\frac{\sin 27^\circ}{\sin 27^\circ} \right)^2 \end{aligned}$$

$$= 1 - 1$$

$$= 0$$

$$(v) \frac{\tan 35^\circ}{\cot 55^\circ} + \frac{\cot 78^\circ}{\tan 12^\circ} - 1$$

Solution:

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We have, [$\because \cot (90 - \theta) = \tan \theta$ and $\tan (90 - \theta) = \cot \theta$]

$$\frac{\tan 35^\circ}{\cot 55^\circ} + \frac{\cot 78^\circ}{\tan 12^\circ} - 1$$

$$= \tan (90^\circ - 35^\circ) / \cot 55^\circ + \cot (90^\circ - 12^\circ) / \tan 12^\circ - 1$$

$$= \cot 55^\circ / \cot 55^\circ + \tan 12^\circ / \tan 12^\circ - 1$$

$$= 1 + 1 - 1$$

$$= 1$$

$$(vi) \frac{\sec 70^\circ}{\operatorname{cosec} 20^\circ} + \frac{\sin 59^\circ}{\cos 31^\circ}$$

Solution:

We have , [$\because \sin (90 - \theta) = \cos \theta$ and $\sec (90 - \theta) = \operatorname{cosec} \theta$]

$$\frac{\sec 70^\circ}{\operatorname{cosec} 20^\circ} + \frac{\sin 59^\circ}{\cos 31^\circ}$$

$$= \sec (90^\circ - 20^\circ) / \operatorname{cosec} 20^\circ + \sin (90^\circ - 31^\circ) / \cos 31^\circ$$

$$= \operatorname{cosec} 20^\circ / \operatorname{cosec} 20^\circ + \cos 12^\circ / \cos 12^\circ$$

$$= 1 + 1$$

$$= 2$$

(vii) $\operatorname{cosec} 31^\circ - \sec 59^\circ$

Solution:

We have,

$$\operatorname{cosec} 31^\circ - \sec 59^\circ$$

Since, $\operatorname{cosec} (90 - \theta) = \cos \theta$

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So,

$$\operatorname{cosec} 31^\circ - \sec 59^\circ = \operatorname{cosec} (90^\circ - 59^\circ) - \sec 59^\circ = \sec 59^\circ - \sec 59^\circ = 0$$

Thus,

$$\operatorname{cosec} 31^\circ - \sec 59^\circ = 0$$

(viii) $(\sin 72^\circ + \cos 18^\circ) (\sin 72^\circ - \cos 18^\circ)$

Solution:

We know that,

$$\sin (90 - \theta) = \cos \theta$$

So, the given can be expressed as

$$(\sin 72^\circ + \cos 18^\circ) (\sin (90 - 18)^\circ - \cos 18^\circ)$$

$$= (\sin 72^\circ + \cos 18^\circ) (\cos 18^\circ - \cos 18^\circ)$$

$$= (\sin 72^\circ + \cos 18^\circ) \times 0$$

$$= 0$$

(ix) $\sin 35^\circ \sin 55^\circ - \cos 35^\circ \cos 55^\circ$

Solution:

We know that,

$$\sin (90 - \theta) = \cos \theta$$

So, the given can be expressed as

$$\sin (90 - 55)^\circ \sin (90 - 35)^\circ - \cos 35^\circ \cos 55^\circ$$

$$= \cos 55^\circ \cos 35^\circ - \cos 35^\circ \cos 55^\circ$$

$$= 0$$

(x) $\tan 48^\circ \tan 23^\circ \tan 42^\circ \tan 67^\circ$

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Solution:

We know that,

$$\tan (90 - \theta) = \cot \theta$$

So, the given can be expressed as

$$\tan (90 - 42)^\circ \tan (90 - 67)^\circ \tan 42^\circ \tan 67^\circ$$

$$= \cot 42^\circ \cot 67^\circ \tan 42^\circ \tan 67^\circ$$

$$= (\cot 42^\circ \tan 42^\circ)(\cot 67^\circ \tan 67^\circ)$$

$$= 1 \times 1 \text{ [}\because \tan \theta \times \cot \theta = 1\text{]}$$

$$= 1$$

(xi) $\sec 50^\circ \sin 40^\circ + \cos 40^\circ \operatorname{cosec} 50^\circ$

Solution:

We know that,

$$\sin (90 - \theta) = \cos \theta \text{ and } \cos (90 - \theta) = \sin \theta$$

So, the given can be expressed as

$$\sec 50^\circ \sin (90 - 50)^\circ + \cos (90 - 50)^\circ \operatorname{cosec} 50^\circ$$

$$= \sec 50^\circ \cos 50^\circ + \sin 50^\circ \operatorname{cosec} 50^\circ$$

$$= 1 + 1 \text{ [}\because \sin \theta \times \operatorname{cosec} \theta = 1 \text{ and } \cos \theta \times \sec \theta = 1\text{]}$$

$$= 2$$

3. Express each one of the following in terms of trigonometric ratios of angles lying between 0° and 45°

(i) $\sin 59^\circ + \cos 56^\circ$ (ii) $\tan 65^\circ + \cot 49^\circ$ (iii) $\sec 76^\circ + \operatorname{cosec} 52^\circ$

(iv) $\cos 78^\circ + \sec 78^\circ$ (v) $\operatorname{cosec} 54^\circ + \sin 72^\circ$ (vi) $\cot 85^\circ + \cos 75^\circ$

(vii) $\sin 67^\circ + \cos 75^\circ$

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Solution:

Using the below trigonometric ratios of complementary angles, we find the required

$$\sin (90 - \theta) = \cos \theta \operatorname{cosec} (90 - \theta) = \sec \theta$$

$$\cos (90 - \theta) = \sin \theta \sec (90 - \theta) = \operatorname{cosec} \theta$$

$$\tan (90 - \theta) = \cot \theta \cot (90 - \theta) = \tan \theta$$

$$(i) \sin 59^\circ + \cos 56^\circ = \sin (90 - 31)^\circ + \cos (90 - 34)^\circ = \cos 31^\circ + \sin 34^\circ$$

$$(ii) \tan 65^\circ + \cot 49^\circ = \tan (90 - 25)^\circ + \cot (90 - 41)^\circ = \cot 25^\circ + \tan 41^\circ$$

$$(iii) \sec 76^\circ + \operatorname{cosec} 52^\circ = \sec (90 - 14)^\circ + \operatorname{cosec} (90 - 38)^\circ = \operatorname{cosec} 14^\circ + \sec 38^\circ$$

$$(iv) \cos 78^\circ + \sec 78^\circ = \cos (90 - 12)^\circ + \sec (90 - 12)^\circ = \sin 12^\circ + \operatorname{cosec} 12^\circ$$

$$(v) \operatorname{cosec} 54^\circ + \sin 72^\circ = \operatorname{cosec} (90 - 36)^\circ + \sin (90 - 18)^\circ = \sec 36^\circ + \cos 18^\circ$$

$$(vi) \cot 85^\circ + \cos 75^\circ = \cot (90 - 5)^\circ + \cos (90 - 15)^\circ = \tan 5^\circ + \sin 15^\circ$$

4. Express $\cos 75^\circ + \cot 75^\circ$ in terms of angles between 0° and 30° .**Solution:**

Given,

$$\cos 75^\circ + \cot 75^\circ$$

Since, $\cos (90 - \theta) = \sin \theta$ and $\cot (90 - \theta) = \tan \theta$

$$\cos 75^\circ + \cot 75^\circ = \cos (90 - 15)^\circ + \cot (90 - 15)^\circ = \sin 15^\circ + \tan 15^\circ$$

Hence, $\cos 75^\circ + \cot 75^\circ$ can be expressed as $\sin 15^\circ + \tan 15^\circ$

5. If $\sin 3A = \cos (A - 26^\circ)$, where $3A$ is an acute angle, find the value of A .**Solution:**

Given,

$$\sin 3A = \cos (A - 26^\circ)$$

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Using $\cos (90 - \theta) = \sin \theta$, we have

$$\sin 3A = \sin (90^\circ - (A - 26^\circ))$$

Now, comparing both L.H.S and R.H.S

$$3A = 90^\circ - (A - 26^\circ)$$

$$3A + (A - 26^\circ) = 90^\circ$$

$$4A - 26^\circ = 90^\circ$$

$$4A = 116^\circ$$

$$A = 116^\circ/4$$

$$\therefore A = 29^\circ$$

6. If A, B, C are the interior angles of a triangle ABC, prove that

(i) $\tan ((C + A)/ 2) = \cot (B/2)$ (ii) $\sin ((B + C)/ 2) = \cos (A/2)$

Solution:

We know that, in triangle ABC the sum of the angles i.e $A + B + C = 180^\circ$

$$\text{So, } C + A = 180^\circ - B \Rightarrow (C + A)/2 = 90^\circ - B/2 \dots\dots (i)$$

$$\text{And, } B + C = 180^\circ - A \Rightarrow (B + C)/2 = 90^\circ - A/2 \dots\dots (ii)$$

$$(i) \text{ L.H.S} = \tan ((C + A)/ 2)$$

$$\Rightarrow \tan ((C + A)/ 2) = \tan (90^\circ - B/2) \text{ [From (i)]}$$

$$= \cot (B/2) \text{ [}\because \tan (90 - \theta) = \cot \theta\text{]}$$

$$= \text{R.H.S}$$

- Hence Proved

$$(ii) \text{ L.H.S} = \sin ((B + C)/2)$$

$$\Rightarrow \sin ((B + C)/ 2) = \sin (90^\circ - A/2) \text{ [From (ii)]}$$

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$$= \cos (A/2)$$

$$= \text{R.H.S}$$

- Hence Proved

7. Prove that:

(i) $\tan 20^\circ \tan 35^\circ \tan 45^\circ \tan 55^\circ \tan 70^\circ = 1$

(ii) $\sin 48^\circ \sec 48^\circ + \cos 48^\circ \operatorname{cosec} 42^\circ = 2$

(iii) $\frac{\sin 70^\circ}{\cos 20^\circ} + \frac{\operatorname{cosec} 20^\circ}{\sec 70^\circ} - 2 \cos 70^\circ \operatorname{cosec} 42^\circ = 0$

(iv) $\frac{\cos 80^\circ}{\sin 10^\circ} + \cos 59^\circ \operatorname{cosec} 31^\circ = 2$

Solution:

(i) Taking L.H.S = $\tan 20^\circ \tan 35^\circ \tan 45^\circ \tan 55^\circ \tan 70^\circ$

$$= \tan (90^\circ - 70^\circ) \tan (90^\circ - 55^\circ) \tan 45^\circ \tan 55^\circ \tan 70^\circ$$

$$= \cot 70^\circ \cot 55^\circ \tan 45^\circ \tan 55^\circ \tan 70^\circ \quad [\because \tan (90 - \theta) = \cot \theta]$$

$$= (\tan 70^\circ \cot 70^\circ)(\tan 55^\circ \cot 55^\circ) \tan 45^\circ \quad [\because \tan \theta \times \cot \theta = 1]$$

$$= 1 \times 1 \times 1 = 1$$

- Hence proved

(ii) Taking L.H.S = $\sin 48^\circ \sec 48^\circ + \cos 48^\circ \operatorname{cosec} 42^\circ$

$$= \sin 48^\circ \sec (90^\circ - 48^\circ) + \cos 48^\circ \operatorname{cosec} (90^\circ - 48^\circ) \quad [\because \sec (90 - \theta) = \operatorname{cosec} \theta \text{ and } \operatorname{cosec} (90 - \theta) = \sec \theta]$$

$$= \sin 48^\circ \operatorname{cosec} 48^\circ + \cos 48^\circ \sec 48^\circ \quad [\because \operatorname{cosec} \theta \times \sin \theta = 1 \text{ and } \cos \theta \times \sec \theta = 1]$$

$$= 1 + 1 = 2$$

- Hence proved

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(iii) Taking the L.H.S,

$$\begin{aligned} & \frac{\sin 70^\circ}{\cos 20^\circ} + \frac{\operatorname{cosec} 20^\circ}{\sec 70^\circ} - 2 \cos 70^\circ \operatorname{cosec} 20^\circ \\ &= \frac{\sin(90^\circ - 20^\circ)}{\cos 20^\circ} + \frac{\operatorname{cosec}(90^\circ - 70^\circ)}{\sec 70^\circ} - 2 \cos(90^\circ - 20^\circ) \operatorname{cosec} 20^\circ \\ &= \frac{\cos 20^\circ}{\cos 20^\circ} + \frac{\sec 70^\circ}{\sec 70^\circ} - 2 \sin 20^\circ \times \frac{1}{\sin 20^\circ} \end{aligned} \quad \left[\begin{array}{l} \sin(90^\circ - \theta) = \cos \theta \\ \operatorname{cosec}(90^\circ - \theta) = \sec \theta \\ \cos(90^\circ - \theta) = \sin \theta \end{array} \right]$$

$$= 1 + 1 - 2$$

$$= 2 - 2$$

$$= 0$$

- Hence proved

(iv) Taking L.H.S,

$$\begin{aligned} & \frac{\cos 80^\circ}{\sin 10^\circ} + \cos 59^\circ \operatorname{cosec} 31^\circ \\ &= \frac{\cos(90^\circ - 10^\circ)}{\sin 10^\circ} + \cos 59^\circ \operatorname{cosec}(90^\circ - 59^\circ) \\ &= \frac{\sin 10^\circ}{\sin 10^\circ} + \cos 59^\circ \sec 59^\circ \end{aligned}$$

$$= 1 + 1$$

$$= 2$$

- Hence proved

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8. Prove the following:

(i) $\sin \theta \sin (90^\circ - \theta) - \cos \theta \cos (90^\circ - \theta) = 0$

Solution:

Taking the L.H.S,

$$\sin \theta \sin (90^\circ - \theta) - \cos \theta \cos (90^\circ - \theta)$$

$$= \sin \theta \cos \theta - \cos \theta \sin \theta \quad [\because \sin (90 - \theta) = \cos \theta \text{ and } \cos (90 - \theta) = \sin \theta]$$

$$= 0$$

(ii)

Solution:

Taking the L.H.S,

$$\frac{\cos(90^\circ - \theta) \sec(90^\circ - \theta) \tan \theta}{\operatorname{cosec}(90^\circ - \theta) \sin(90^\circ - \theta) \cot(90^\circ - \theta)} + \frac{\tan(90^\circ - \theta)}{\cot \theta}$$

$$= \frac{\sin \theta \operatorname{cosec} \theta \tan \theta}{\sec \theta \cos \theta \tan \theta} + \frac{\cot \theta}{\cot \theta}$$

$$= \frac{1 \times \tan \theta}{1 \times \tan \theta} + 1 = \frac{\tan \theta}{\tan \theta} + 1$$

$$[\because \operatorname{cosec} \theta \times \sin \theta = 1 \text{ and } \cos \theta \times \sec \theta = 1]$$

$$= 1 + 1$$

$$= 2 = \text{R.H.S}$$

- Hence Proved

(iii)

Solution:

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Taking the L.H.S, [$\because \tan (90^\circ - \theta) = \cot \theta$]

$$\begin{aligned} \text{L.H.S.} &= \frac{\tan(90^\circ - A) \cot A}{\operatorname{cosec}^2 A} - \cos^2 A \\ &= \frac{\cot A \cot A}{\operatorname{cosec}^2 A} - \cos^2 A \\ &= \frac{\cot^2 A}{\operatorname{cosec}^2 A} - \cos^2 A = \frac{\frac{\cos^2 A}{\sin^2 \theta}}{\frac{1}{\sin^2 A}} - \cos^2 A \\ &= \frac{\cos^2 A \times \sin^2 A}{\sin^2 A \times 1} - \cos^2 A = \cos^2 A - \cos^2 A \end{aligned}$$

= 0 = R.H.S

- Hence Proved

(iv)

Solution:

Taking L.H.S, [$\because \sin (90 - \theta) = \cos \theta$ and $\cos (90 - \theta) = \sin \theta$]

= $\sin^2 A$ = R.H.S

- Hence Proved

(v) $\sin (50^\circ + \theta) - \cos (40^\circ - \theta) + \tan 1^\circ \tan 10^\circ \tan 20^\circ \tan 70^\circ \tan 80^\circ \tan 89^\circ = 1$

Solution:

Taking the L.H.S,

= $\sin (50^\circ + \theta) - \cos (40^\circ - \theta) + \tan 1^\circ \tan 10^\circ \tan 20^\circ \tan 70^\circ \tan 80^\circ \tan 89^\circ$

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$$= [\sin (90^\circ - (40^\circ - \theta))] - \cos (40^\circ - \theta) + \tan (90 - 89)^\circ \tan (90 - 80)^\circ \tan (90 - 70)^\circ \tan 70^\circ \tan 80^\circ \tan 89^\circ [\because \sin (90 - \theta) = \cos \theta]$$

$$= \cos (40^\circ - \theta) - \cos (40^\circ - \theta) + \cot 89^\circ \cot 80^\circ \cot 70^\circ \tan 70^\circ \tan 80^\circ \tan 89^\circ [\because \tan (90^\circ - \theta) = \cot \theta]$$

$$= 0 + (\cot 89^\circ \times \tan 89^\circ) (\cot 80^\circ \times \tan 80^\circ) (\cot 70^\circ \times \tan 70^\circ)$$

$$= 0 + 1 \times 1 \times 1 [\because \tan \theta \times \cot \theta = 1]$$

$$= 1 = \text{R.H.S}$$

- Hence Proved



Chapterwise RD Sharma Solutions for Class 10 Maths :

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- Chapter 2–Polynomials
- Chapter 3–Pair of Linear Equations In Two Variables
- Chapter 4–Triangles
- Chapter 5–Trigonometric Ratios
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About RD Sharma

RD Sharma isn't the kind of author you'd bump into at lit fests. But his bestselling books have helped many CBSE students lose their dread of maths. Sunday Times profiles the tutor turned internet star

He dreams of algorithms that would give most people nightmares. And, spends every waking hour thinking of ways to explain concepts like 'series solution of linear differential equations'. Meet Dr Ravi Dutt Sharma — mathematics teacher and author of 25 reference books — whose name evokes as much awe as the subject he teaches. And though students have used his thick tomes for the last 31 years to ace the dreaded maths exam, it's only recently that a spoof video turned the tutor into a YouTube star.

R D Sharma had a good laugh but said he shared little with his on-screen persona except for the love for maths. "I like to spend all my time thinking and writing about maths problems. I find it relaxing," he says. When he is not writing books explaining mathematical concepts for classes 6 to 12 and engineering students, Sharma is busy dispensing his duty as vice-principal and head of department of science and humanities at Delhi government's Guru Nanak Dev Institute of Technology.

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